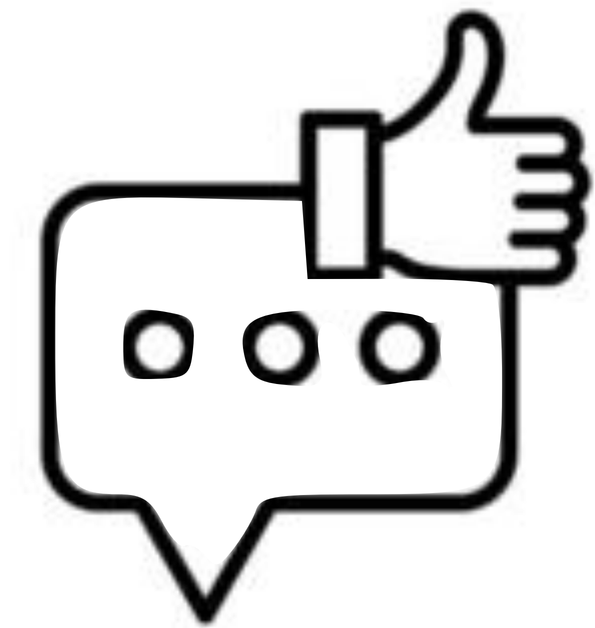
Niv Dayan - CSC2525: Research Topics in Database Management

Logistics

Projects due
on April 15

Exams on
April 30



Course
Evaluation

BitWeaving

SIGMOD 2013

BitWeaving
SIGMOD 2013

Cool bit manipulation techniques

Assume column-store

(Each column in table is separate)

Birth Year	Name	Address
1970	…	…
1981	…	…
2000	…	…
1976	…	…
…	…	…

Birth Year **(BY)**

1970

1981

2000

1976

…

Example Query

Select * where **BY < X and BY > Y**

Birth Year

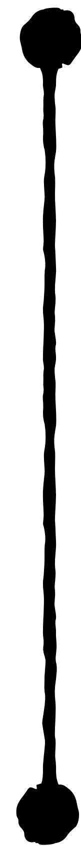
1970

1981

2000

1976

...



How to encode?

Birth Year	**4 byte integer**
1970	0000000000000000 0000011110110010
1981	0000000000000000 0000011110111101
2000	0000000000000000 0000011111010000
1976	0000000000000000 0000011110111000
…	

Birth Year	**4 byte integer**
1970	0000000000000000 0000011110110010
1981	0000000000000000 0000011110111101
2000	0000000000000000 0000011111010000
1976	0000000000000000 0000011110111000
…	

Problem?

Birth Year	4 byte integer
1970	**0000000000000000 00000**11110110010
1981	**0000000000000000 00000**11110111101
2000	**0000000000000000 00000**11111010000
1976	**0000000000000000 00000**11110111000
…	

Space wastage

Birth Year	4 byte integer
1970	**0000000000000000 00000**11110110010
1981	**0000000000000000 00000**11110111101
2000	**0000000000000000 00000**11111010000
1976	**0000000000000000 00000**11110111000
…	

Space wastage

Worse scan performance!

Birth Year	**2 byte integer**
1970	0000011110110010
1981	0000011110111101
2000	0000011111010000
1976	0000011110111000
…	

Birth Year	**2 byte integer**
1970	0000011110110010
1981	0000011110111101
2000	0000011111010000
1976	0000011110111000
…	

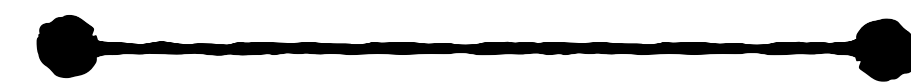
2x faster :)

Birth Year	**2 byte integer**
1970	0000011110110010
1981	0000011110111101
2000	0000011111010000
1976	0000011110111000
…	**Problem?**

Birth Year	**2 byte integer**
1970	**00000**11110110010
1981	**00000**11110111101
2000	**00000**11111010000
1976	**00000**11110111000
…	

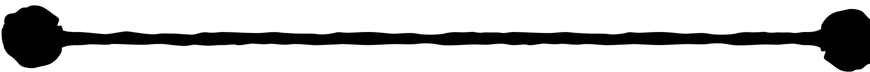
Leading zeros

Birth Year	**2 byte integer**
1970	00000**11110110010**
1981	00000**11110111101**
2000	00000**11111010000**
1976	00000**11110111000**
…	



Narrow range
e.g., 1900 - 2025

Birth Year	**2 byte integer**
1970	00000**11110110010**
1981	00000**11110111101**
2000	00000**11111010000**
1976	00000**11110111000**
…	



Narrow range
e.g., 1900 - 2025

Most values aren’t used

Birth Year	**2 byte integer**
1970	00000**11110110010**
1981	00000**11110111101**
2000	00000**11111010000**
1976	00000**11110111000**
…	

Solutions? :)

Solutions from CSC443

0
1
1
0

Bit-vector encoding

Run-Length Encoding

Dictionary Encoding

0
1
1
0

Bit-vector encoding

Run-Length Encoding

Frame of Reference Encoding

Dictionary Encoding

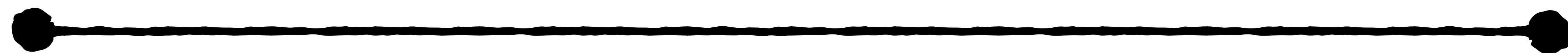
0
1
1
0

Bit-vector encoding

Run-Length Encoding

Frame of Reference Encoding

Dictionary Encoding



Less Relevant for today

Quick Review

Frame of Reference Encoding

Dictionary Encoding

Frame of Reference Encoding

Birth Year

1970

1981

2000

1976

…

Frame of Reference Encoding

Birth Year

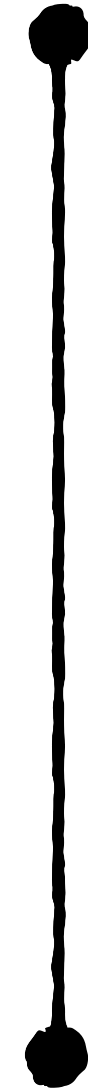
1970

1981

2000

1976

…



Find min
e.g., 1970

Frame of Reference Encoding

Birth Year		**Store differences**
1970	**- 1970 =**	**0**
1981	**- 1970 =**	**11**
2000	**- 1970 =**	**30**
1976	**- 1970 =**	**6**
…		

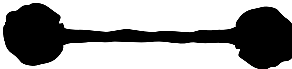
Frame of Reference Encoding

Birth Year	**Store differences**
1970	00000000
1981	00001011
2000	00011110
1976	00000110
…	

Down to 1 byte :)

Frame of Reference Encoding

Birth Year	Store differences
1970	**00**000000
1981	**00**001011
2000	**00**011110
1976	**00**000110
...	



Still wasting some space & speed

Quick Review

Frame of Reference Encoding

Dictionary Encoding

Dictionary Encoding

Birth Year
1970
1981
2000
1970
1970
2000

Birth Year

1970

1981

2000

1970

1970

2000

Dictionary

1970	**0**
1981	**1**
2000	**2**

Birth Year	Dictionary		**Compressed column**
1970	1970	0	**0**
1981	1981	1	**1**
2000	2000	2	**2**
1970			**1**
1970			**1**
2000			**2**

Birth Year	Compressed column
1970	**0**
1981	**1**
2000	**2**
1970	**1**
1970	**1**
2000	**2**

Order-Preserving Dictionary

1970	**0**
1981	**1**
2000	**2**

Order-Preserving Dictionary

Birth Year
1970
1981
2000
1970
1970
2000

Sorted ↓

1970	0
1981	1
2000	2

↓ **Sorted**

Compressed column
0
1
2
1
1
2

Birth Year
1970
1981
2000
1970
1970
2000

Order-Preserving Dictionary

Sorted ↓ | Sorted ↓

1970	0
1981	1
2000	2

Compressed column
0
1
2
1
1
2

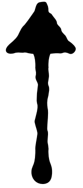
Select * where year > 1981

Birth Year	Order-Preserving Dictionary		Compressed column
1970	1970	0	**0**
1981	**1981**	**1**	**1**
2000	2000	2	**2**
1970			**1**
1970			**1**
2000			**2**

Replace with code

Select * where year > **1**

Birth Year	Order-Preserving Dictionary		**Compressed column**
1970	1970	0	**0000 0000**
1981	1981	1	**0000 0001**
2000	2000	2	**0000 0010**
1970			**0000 0001**
1970			**0000 0001**
2000			**0000 0010**



Encode as 1 byte…

Quick Review

Frame of Reference Encoding

Dictionary Encoding

Problems

Checking Whole Codes

Wasted Space

Checking Whole Codes

Dec
1
10
7
11

Checking Whole Codes

Dec	Binary
1	0001
10	1010
7	0111
11	1011

Dec	Binary
1	0001
10	1010
7	0111
11	1011

Select * where c ≥ 12 (1100)

	Dec	Binary
Scan each code →	1	0001
	10	1010
	7	0111
	11	1011

Select * where c ≥ 12 (1100)

Problem?

	Dec	Binary
	1	0001
	10	1010
	7	0111
Scan each code →	11	1011

Select * where c ≥ 12 (1100)

Problem?

We could have known after only 2 bits per code that none qualify

Dec	Binary
1	**00**01
10	**10**10
7	**01**11
11	**10**11

Select * where c ≥ 12 **(1100)**

Problems

Checking
Whole Codes

Wasted
Space

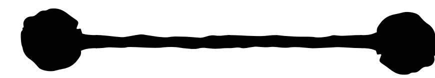
Wasted Space

00000 000

00000 101

00000 011

00000 110



Leading zeros waste space force traversing more data

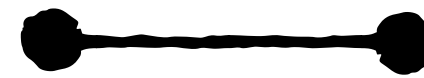
Wasted Space

00000 000

00000 101

00000 011

00000 110



Leading zeros waste space force traversing more data

Solutions? :)

Three Straw-Man Solutions

Dense Packing

Align & Pad

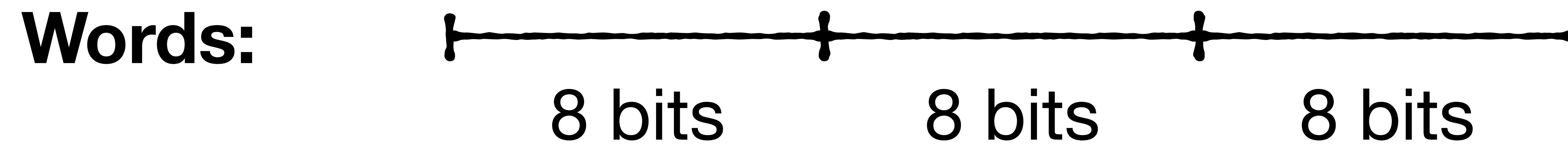
Pack, Align & Pad

Dense Packing

Codes: **000** 101 **011** 110 **111** 010 **111**

Dense Packing

Codes: **000** 101 **011** 110 **111** 010 **111**

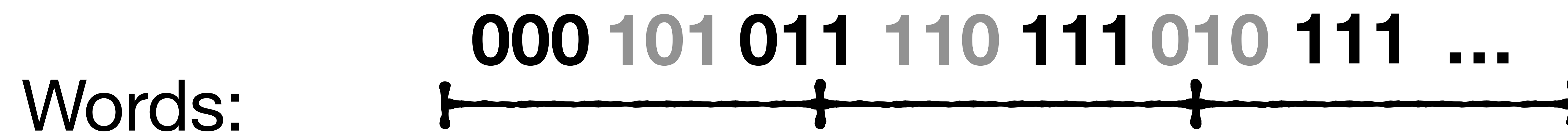


Assume 8 bit words - in reality 64

Dense Packing

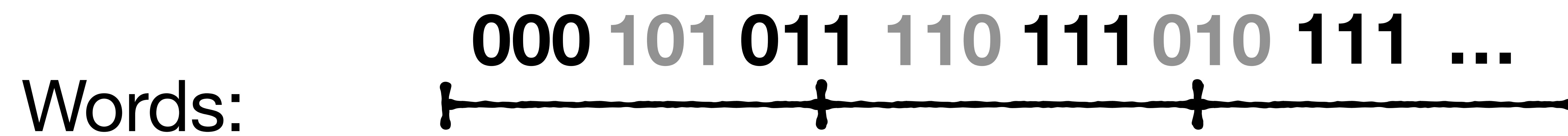
Words:

Dense Packing



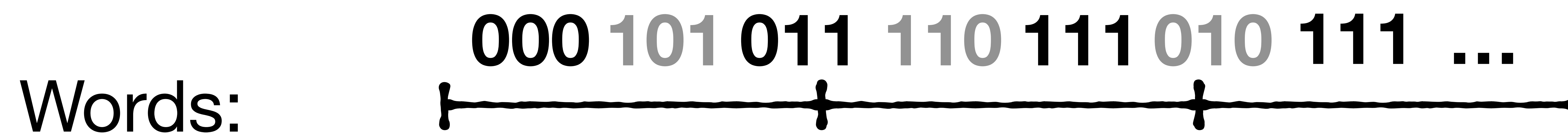
Problems?

Dense Packing



Problems? **The processor reads at word granularity**

Dense Packing



Problems? The processor reads at word granularity

Hard to run CPU instructions (=, >, <) on codes due to their irregular offsets within words and no alignment

Three Straw-Man Solutions

Dense Packing

Align & Pad

Pack, Align & Pad

Align & Pad (every 8 bits)

Align & Pad (every 16 bits)

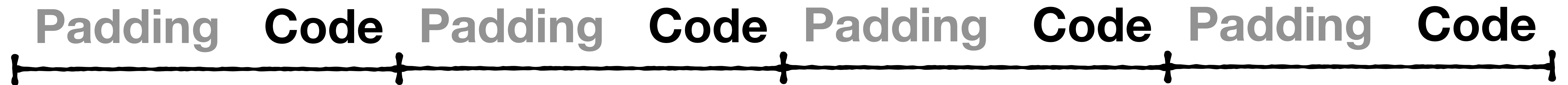
e.g., with 11 bit codes

Align & Pad (every 32 bits)

e.g., with 20 bit codes

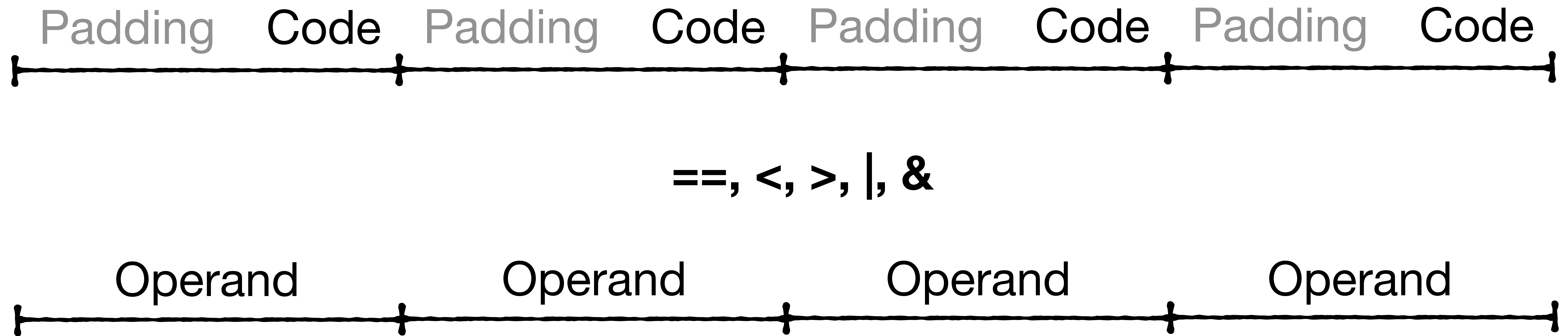
Align & Pad

Allows AVX instructions (SIMD)



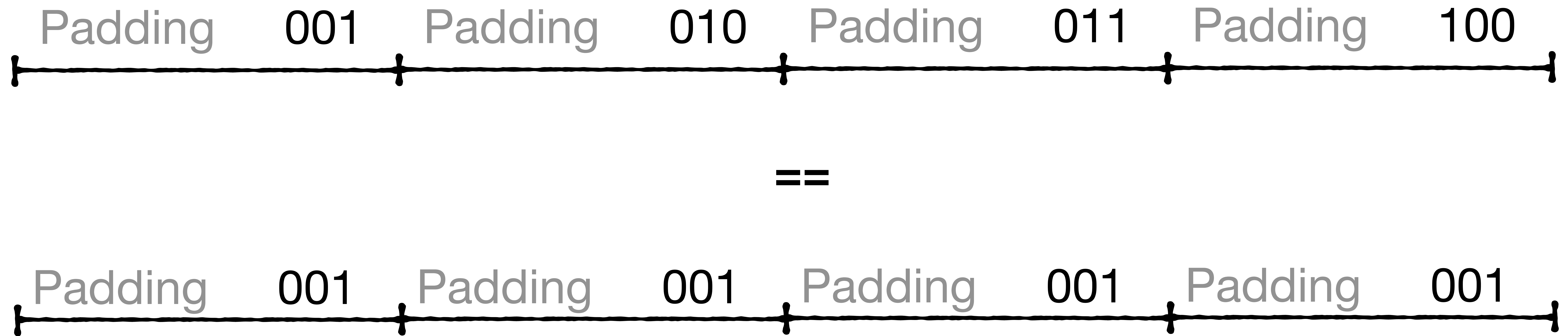
Align & Pad

Allows AVX instructions (SIMD)



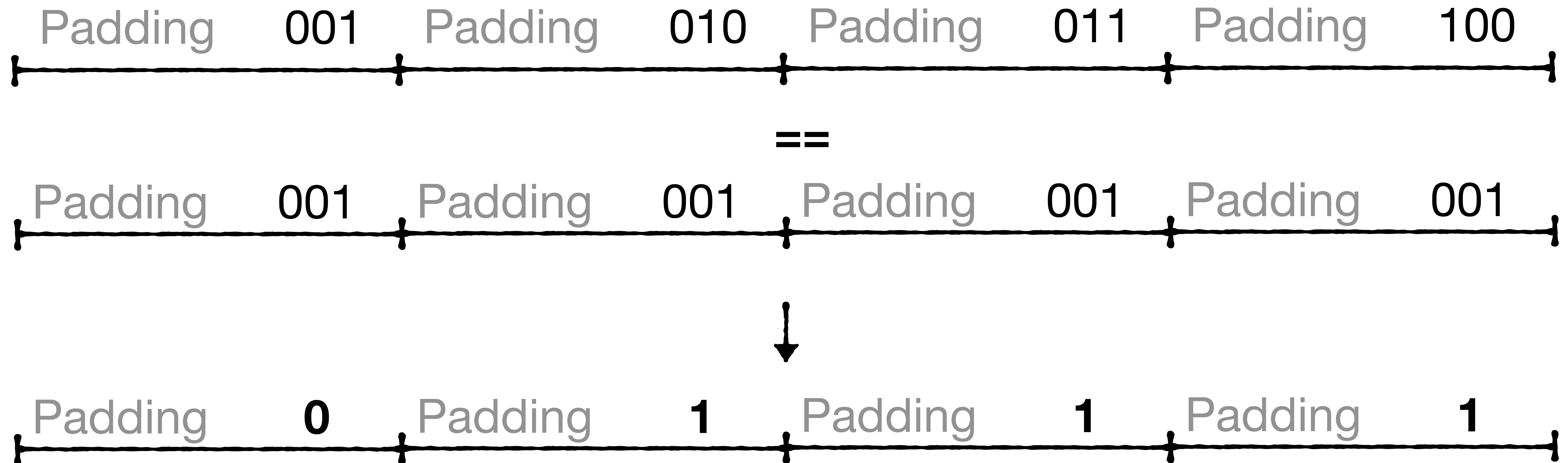
Align & Pad

Allows AVX instructions (SIMD)

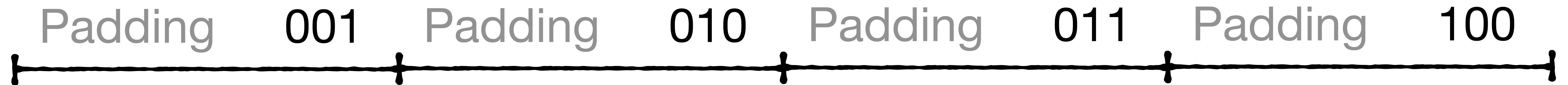


Align & Pad

Allows AVX instructions (SIMD)



Align & Pad



Padding wastes space and slows down scans

Three Straw-Man Solutions

Dense
Packing

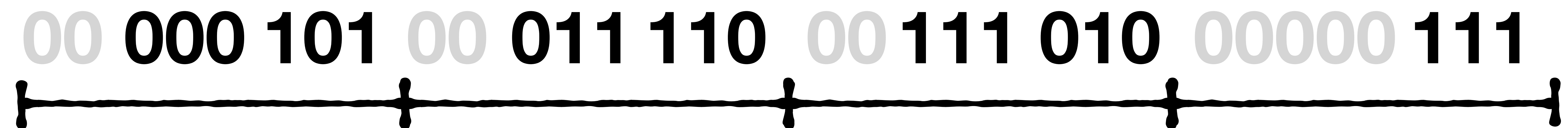
Align & Pad

Pack, Align & Pad

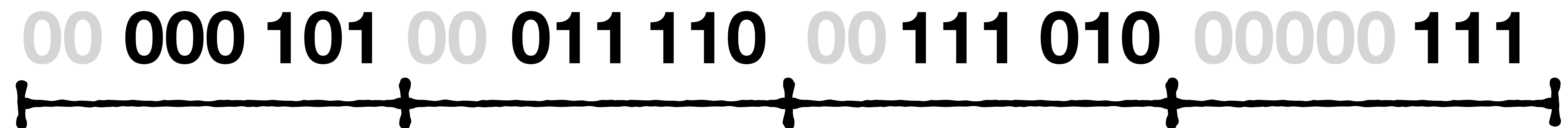
Pack, Align & Pad

Pack, Align & Pad

Pack only as many codes into each word as would fit



wastes some space, but since word size is usually 64 bits, only a bit of space is wasted at the end



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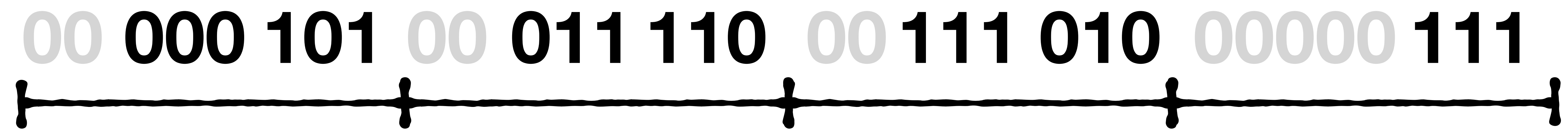

Problems?

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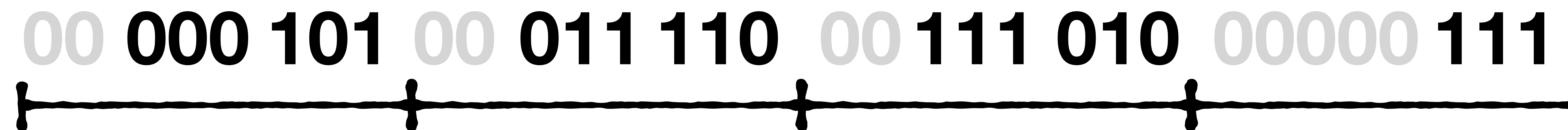
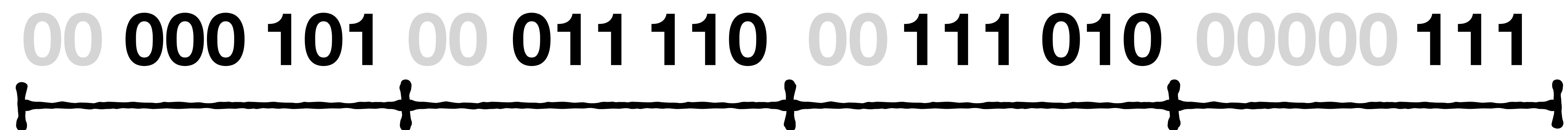


Problems?

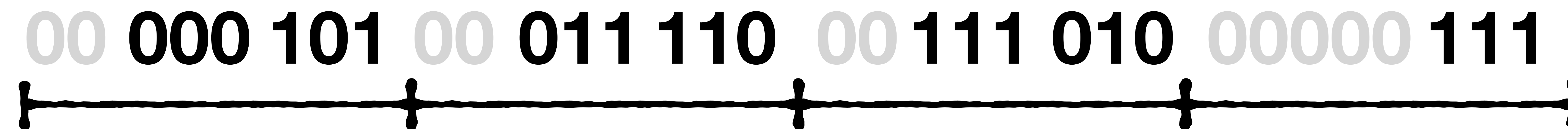
Can’t use SIMD



Problems? Can’t use SIMD

Looping over each code during query is CPU-intensive

```
for (int i = 0; i < words; i++)
    for (int j = 0; j < word_size; j += code_size)
```

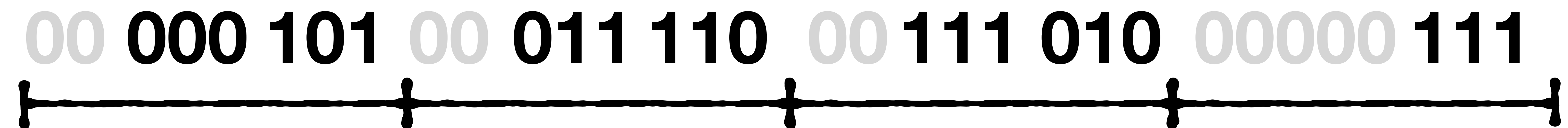


Problems?

Can’t use SIMD

Looping over each code during query is CPU-intensive

```
for (int i = 0; i < words; i++)
    for (int j = 0; j < word_size; j += code_size)
        code = extract_code(j, j + code_size)
```



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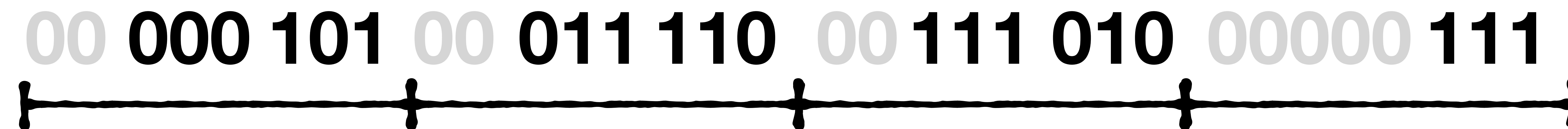
```
for (int i = 0; i < words; i++)
    for (int j = 0; j < word_size; j += code_size)
        code = extract_code(j, j + code_size)
        If( selection_predicate(code) )
            record result
```



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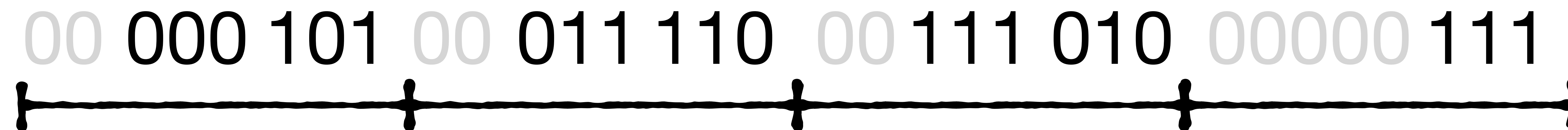


Can we do better in terms of CPU?

Problems

Wasted Space

Checking whole Codes

BitWeaving: Fast Scans for Main Memory Data Processing

Yinan Li, Jignesh M. Patel

SIGMOD 2013

BitWeaving: Fast Scans for Main Memory Data Processing

Yinan Li, Jignesh M. Patel

SIGMOD 2013

use bitwise operations to achieve parallelism at word level

BitWeaving: Fast Scans for Main Memory Data Processing

Horizontal

Vertical

Horizontal BitWeaving

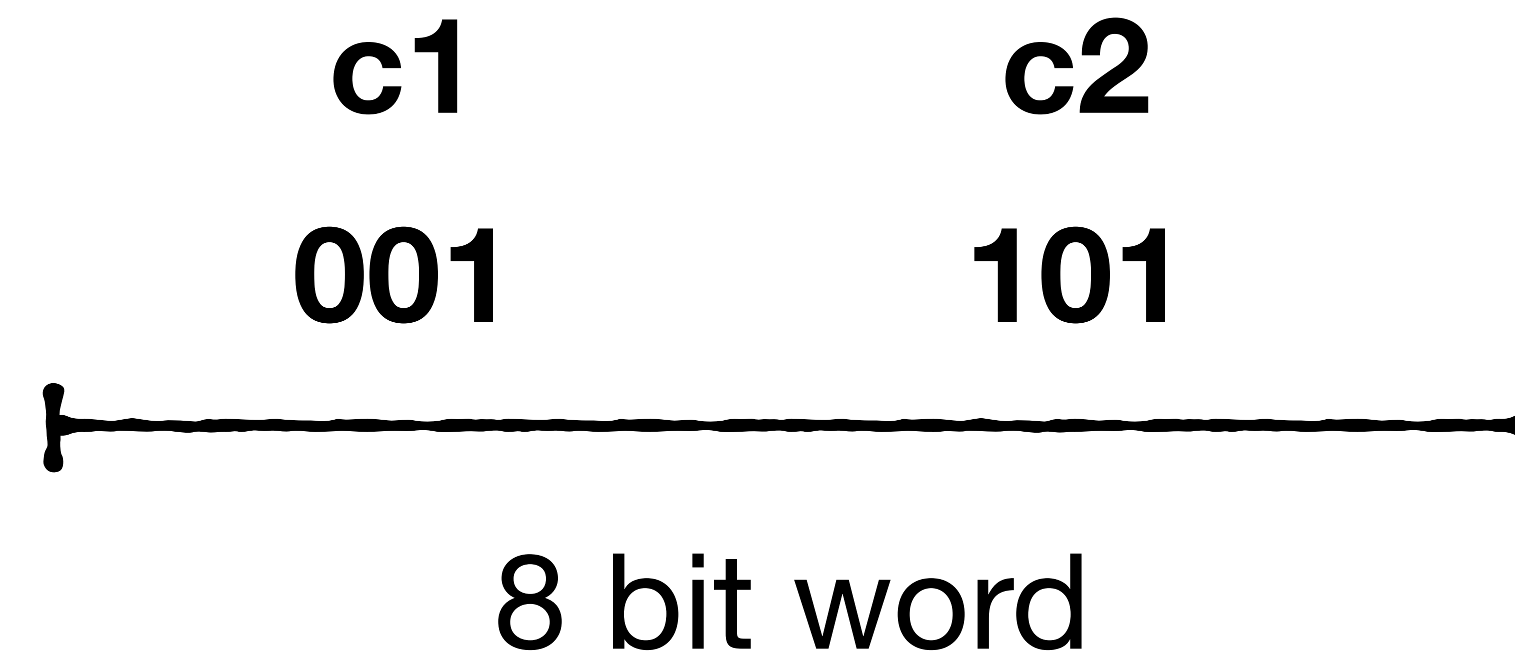
Column codes

c1	001
c2	101

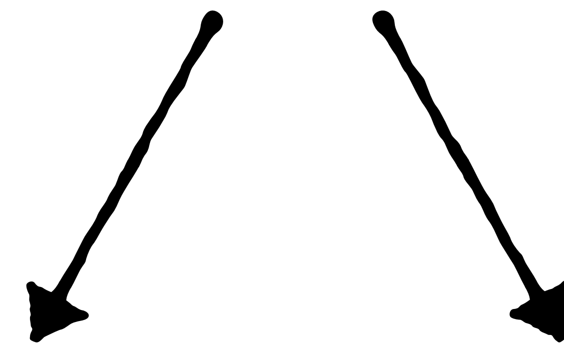
8 bit word

c1
c2
001
101
8 bit word

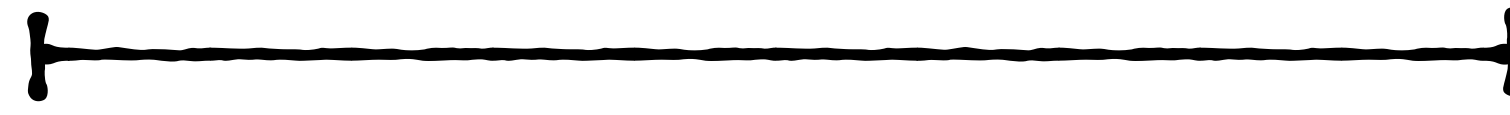
Similar to “Pack, Align & Pad”, except…



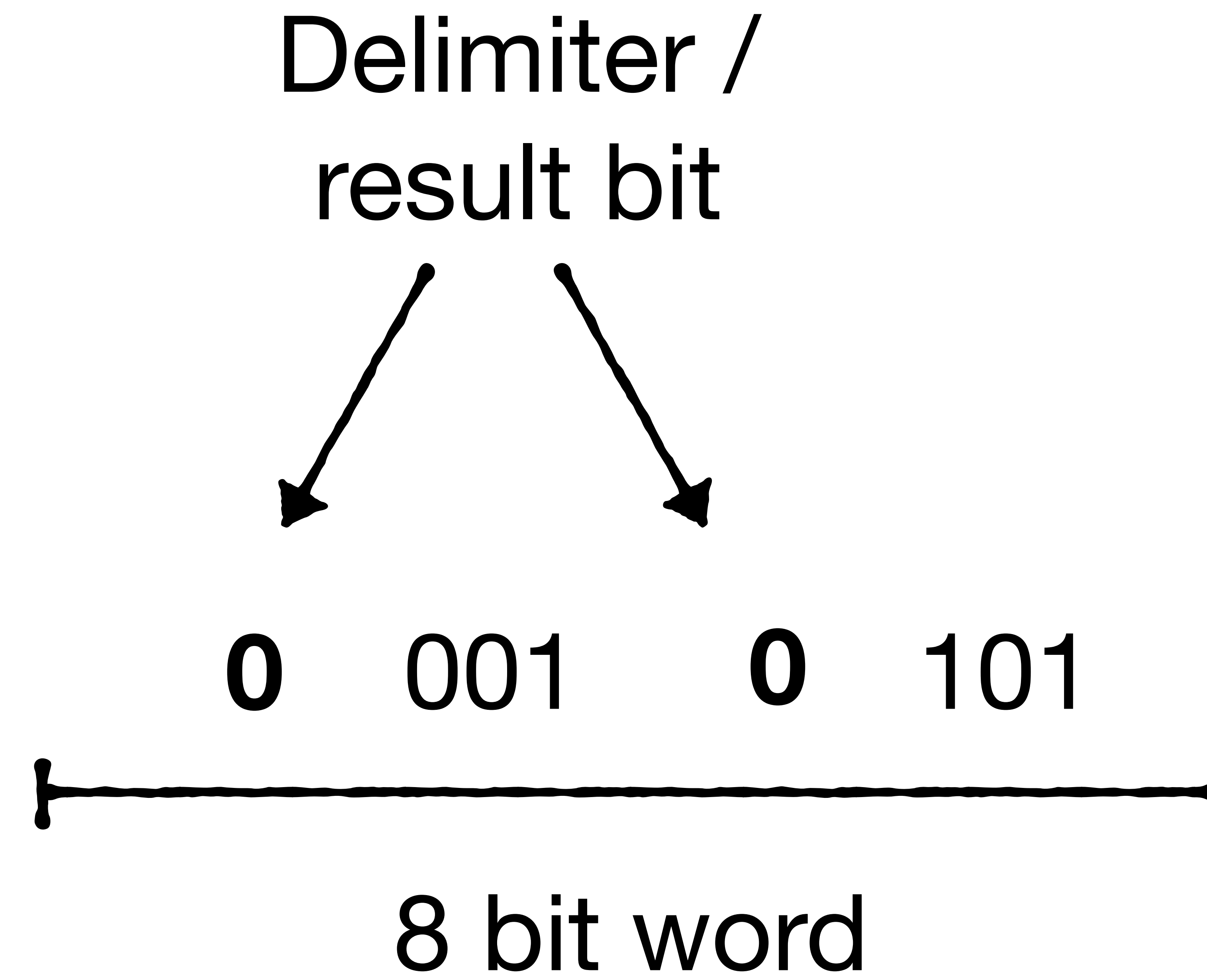
Delimiter / result bit



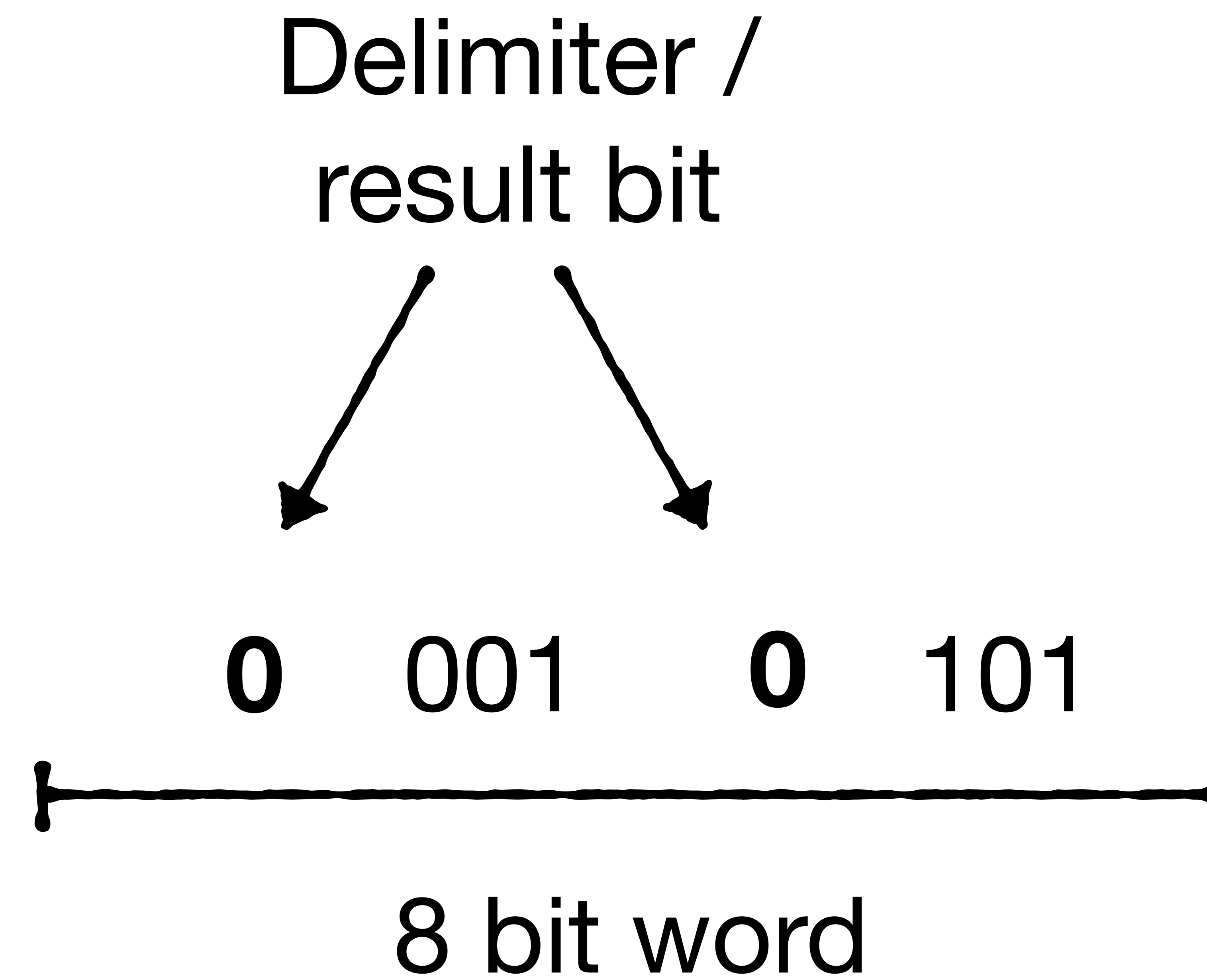
0 001 **0** 101



8 bit word



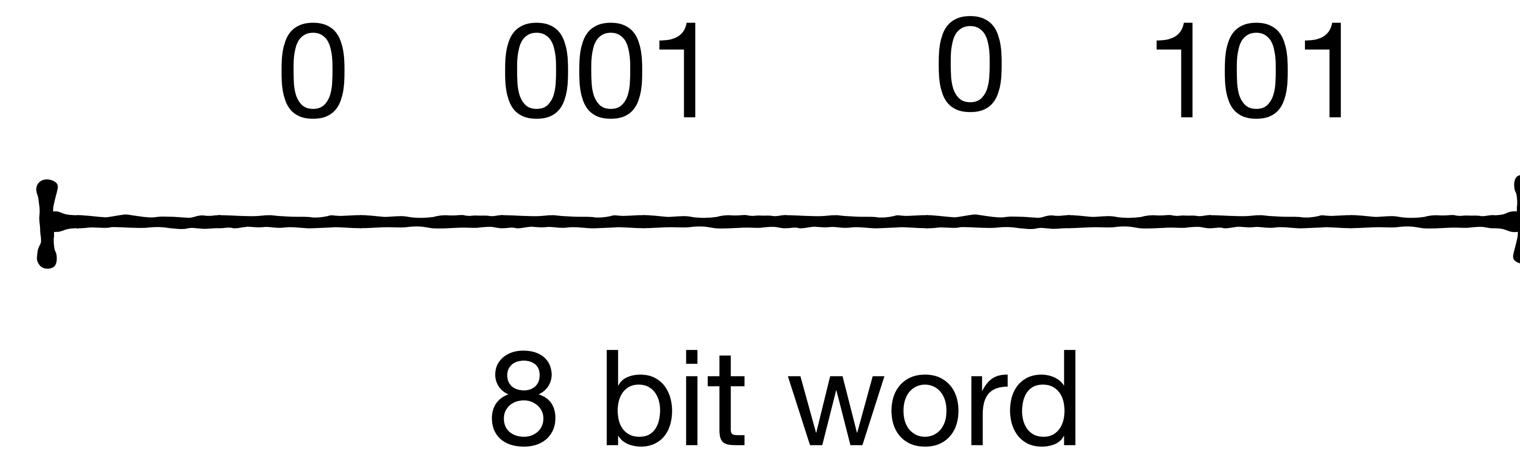
Evaluate predicate (==, <, >, |, &) on all codes in a word in parallel



Evaluate predicate (==, <, >, |, &) on all codes in a word in parallel

Store result for each code in result bit

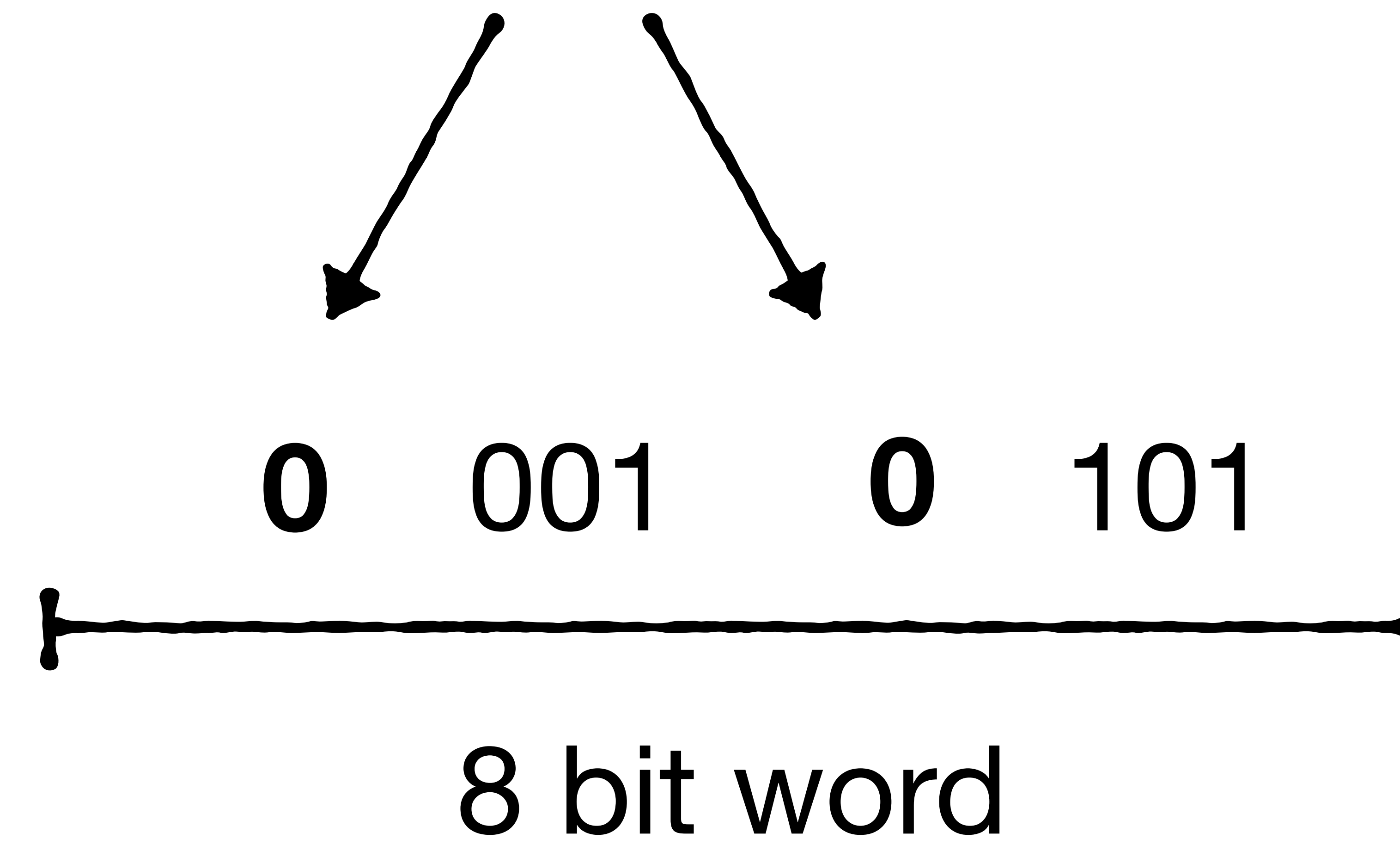
Let’s consider ≠



Let's consider ≠

e.g., Select * where X ≠ constant

Run bitwise operations on word such that delimiter for each code will be 1 if unequal



$$\mathbf{X} \neq \mathbf{Y} \quad \text{iff} \quad \mathbf{X} \oplus \mathbf{Y} \neq \mathbf{0}$$

$X \neq Y$ iff $X \oplus Y \neq 0$

0 0 1 1

$\oplus$

0 0 1 1

=

0 0 0 0

$X \neq Y$ iff $X \oplus Y \neq 0$

$$
\begin{array}{c}
0\ 0\ 1\ 1 \\
\oplus \\
0\ 0\ 1\ \mathbf{0} \\
\mathbf{=} \\
0\ 0\ 0\ \mathbf{1}
\end{array}
$$

$X \neq Y$ iff $X \oplus Y \neq 0$

iff $\mathbf{(X \oplus Y) + 01^K = 1{*}^K}$

$$\begin{array}{c} 0\ 0\ 1\ 1 \\ \oplus \\ 0\ 0\ 1\ 0 \\ \mathbf{=} \\ 0\ 0\ 0\ 1 \end{array}$$

$X \neq Y$ iff $X \oplus Y \neq 0$

iff $\mathbf{(X \oplus Y) + 01^K = 1{*}^K}$

0 0 1 1

⊕

0 0 1 0

0 0 0 1

+

0 1 1 1

=

1 0 0 0

$X \neq Y$ iff $X \oplus Y \neq 0$

iff $(X \oplus Y) + 01^K = 1*^K$

0 0 1 1

$\oplus$

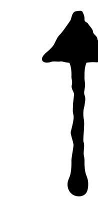
0 0 1 0

+

0 1 1 1

=

1 0 0 0



Always 1 if X ≠ Y

$X \neq Y$ iff $X \oplus Y \neq 0$

iff $(X \oplus Y) + 01^K = 1{*}^K$

0 0 1 1

$\oplus$

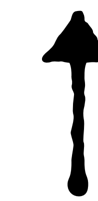
0 0 1 1

$+$

0 1 1 1

=

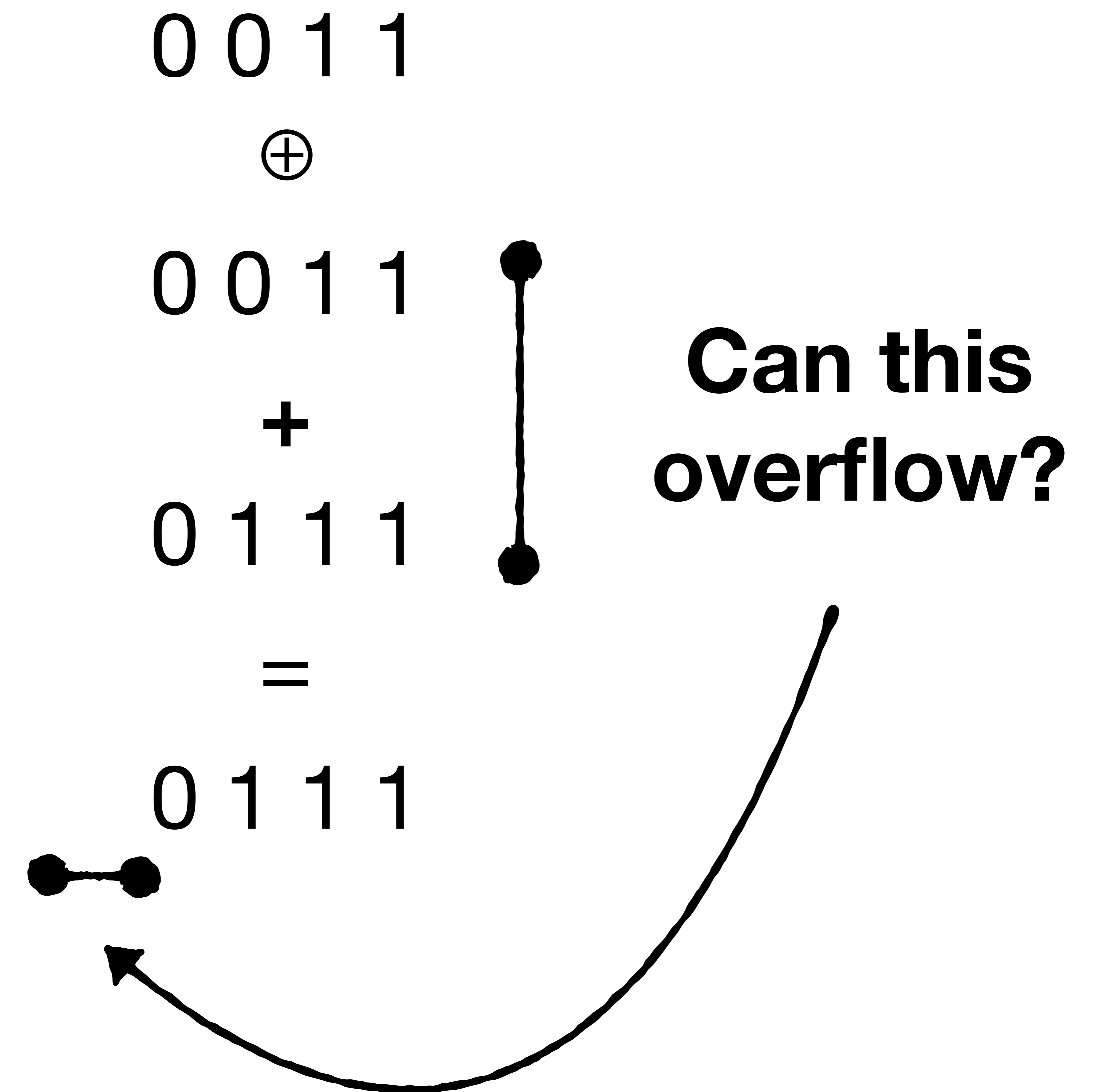
0 1 1 1



Always 0 if X = Y

$$X \neq Y \quad \text{iff} \quad X \oplus Y \neq 0$$

$$\text{iff} \quad (X \oplus Y) + 01^K = 1*^K$$



$X \neq Y$ iff $X \oplus Y \neq 0$

iff $(X \oplus Y) + 01^K = 1*^K$

0 0 1 1

$\oplus$

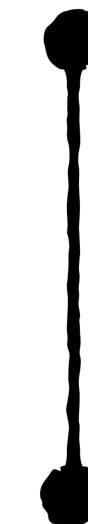
0 0 1 1

+

0 1 1 1

=

0 1 1 1



Can this overflow?

No :)

addition of 2 integers never overflows by more than one bit

e.g., 0111 + 0111 = 1110

$X \neq Y$ iff $X \oplus Y \neq 0$

iff $(X \oplus Y) + 01^K = 1{*}^K$

0 0 1 1

$\oplus$

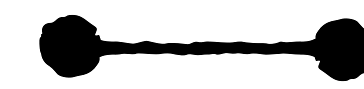
0 0 1 1

+

0 1 1 1

=

0 **1 1 1**



Always 1^K iff X = Y

$X \neq Y$ iff $X \oplus Y \neq 0$

iff $(X \oplus Y) + 01^K = 1*^K$

0 0 1 1

$\oplus$

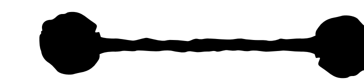
0 1 0 1

+

0 1 1 1

=

1 1 0 1



Can be anything if $X \neq Y$

$X \neq Y$ iff $X \oplus Y \neq 0$

iff $(X \oplus Y) + 01^K = 1*^K$

iff $((X \oplus Y) + 01^K) \wedge \mathbf{10^K = 10^K}$

0 0 1 1

$\oplus$

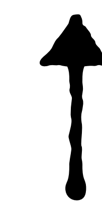
0 1 0 1

+

0 1 1 1

=

1 1 0 1



Reset

$X \neq Y$ iff $X \oplus Y \neq 0$

iff $(X \oplus Y) + 01^K = 1*^K$

iff $((X \oplus Y) + 01^K) \wedge 10^K = 10^K$

0 0 1 1

$\oplus$

0 1 0 1

+

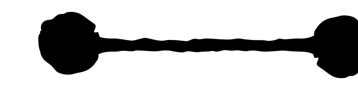
0 1 1 1

$\wedge$

1 0 0 0

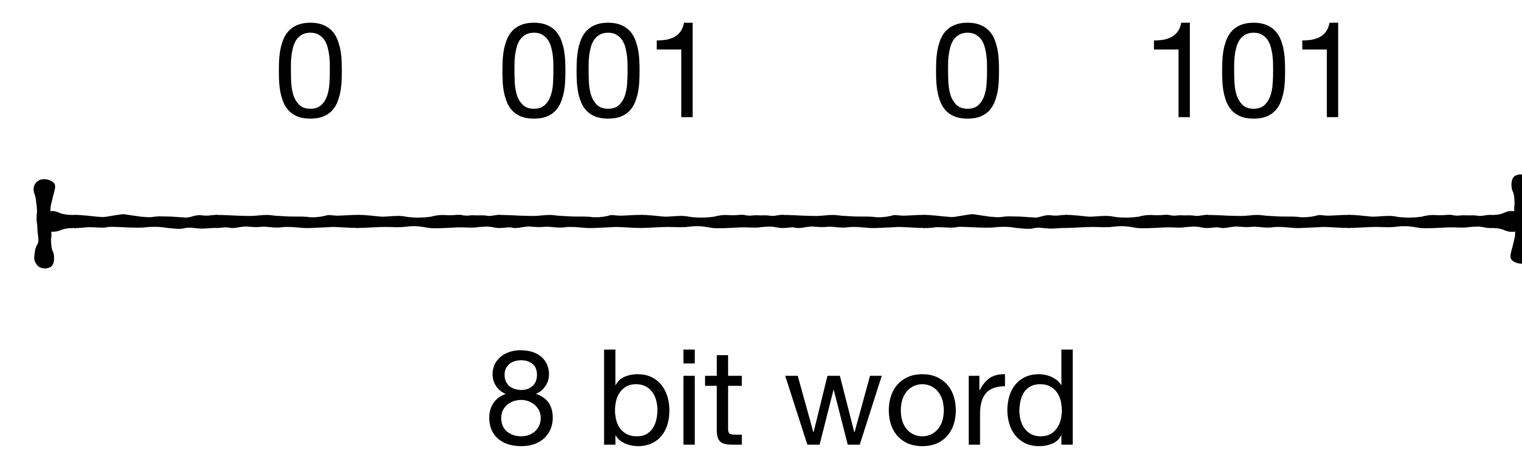
=

1 0 0 0



Reset

Now let's apply this in parallel on all codes in a word



Now let's apply this in parallel on all codes in a word

Select * where X != 5

Now let’s apply this in parallel on all codes in a word

Select * where X != 5

word	0	001	0	101
		$\oplus$		$\oplus$
Constant (5)	**0**	**101**	**0**	**101**

Now let's apply this in parallel on all codes in a word

Select * where X != 5

word	0	001	0	101
		⊕		⊕
Constant (5)	0	101	0	101
		+		**+**
Mask	**0**	**111**	**0**	**111**

Now let’s apply this in parallel on all codes in a word

Select * where X != 5

word	0	001	0	101
		⊕		⊕
Constant (5)	0	101	0	101
		+		+
Mask	0	111	0	111
		∧		∧
-Mask	**1**	**000**	**1**	**000**

Now let's apply this in parallel on all codes in a word

Select * where X != 5

word	0	001	0	101
		⊕		⊕
Constant (5)	0	101	0	101
		+		+
Mask	0	111	0	111
		∧		∧
-Mask	1	000	1	000
		=		=
Result	**1**	000	**0**	000

Can apply on multiple words in a cache line using SIMD

	word 1				word 2			
word	0	001	0	101	0	101	0	000
		⊕		⊕		⊕		⊕
Constant (5)	0	101	0	101	0	101	0	101
		+		+		+		+
Mask	0	111	0	111	0	111	0	111
		^		^		^		^
-Mask	1	000	1	000	1	000	1	000
		=		=		=		=
Result	**1**	000	**0**	000	**0**	000	**1**	000

Word-Level Parallelism

Vectorization (SIMD)

Word-Level Parallelism

Within single machine word using general purpose registers & instructions

Vectorization (SIMD)

Across words in a cache line using specialized instructions & registers

Word-Level Parallelism

Within single machine word using general purpose registers & instructions

Vectorization (SIMD)

Across words in a cache line using specialized instructions & registers

Compatible using careful design :)

How about range predicates?

Select * where X < Y

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$$\mathbf{X = Y \ \ iff \ \ (X \oplus 01^K) + Y = 01^K}$$

How about range predicates?

Select * where X < Y

$X = Y$ iff $(X \oplus 01^K) + Y = 01^K$

X	**0 1 1 0**
	$\oplus$
01^K	**0 1 1 1**
	+
Y	**0 1 1 0**

How about range predicates?

Select * where X < Y

$X = Y$ iff $(X \oplus 01^K) + Y = 01^K$

X	0 1 1 0	
	⊕	**0 0 0 1**
01^K	0 1 1 1	
	+	
Y	**0 1 1 0**	

How about range predicates?

Select * where X < Y

$X = Y$ iff $(X \oplus 01^K) + Y = 01^K$

X	0 1 1 0
	⊕
01^K	0 1 1 1
	+
Y	0 1 1 0
	=
	0 1 1 1

0 0 0 1

How about range predicates?

Select * where X < Y

$X = Y$ iff $(X \oplus 01^K) + Y = 01^K$

X	**0 1 1 0**
	$\oplus$
01^K	0 1 1 1
	+
Y	**0 1 1 0**
	=
	0 1 1 1

0 0 0 1

Always iff X=Y

How about range predicates?

Select * where $X < Y$

$X = Y$ iff $(X \oplus 01^K) + Y = 01^K$

X	0 1 1 0
	$\oplus$
01^K	0 1 1 1
	+
Y	0 1 1 0
	=
	0 1 1 1

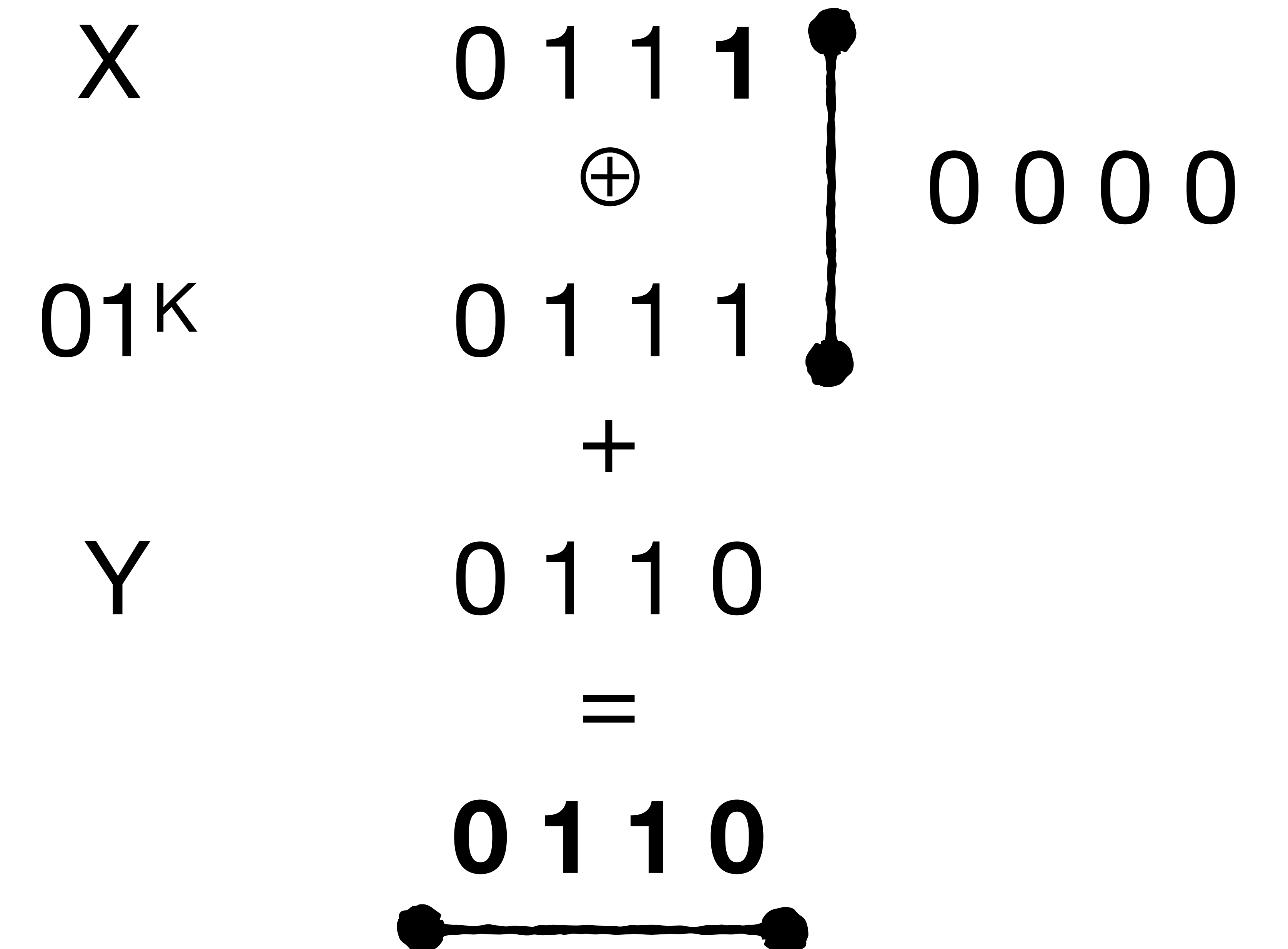
0 0 0 1

If X>Y, result decreases

How about range predicates?

Select * where X < Y

$X = Y$ iff $(X \oplus 01^K) + Y = 01^K$

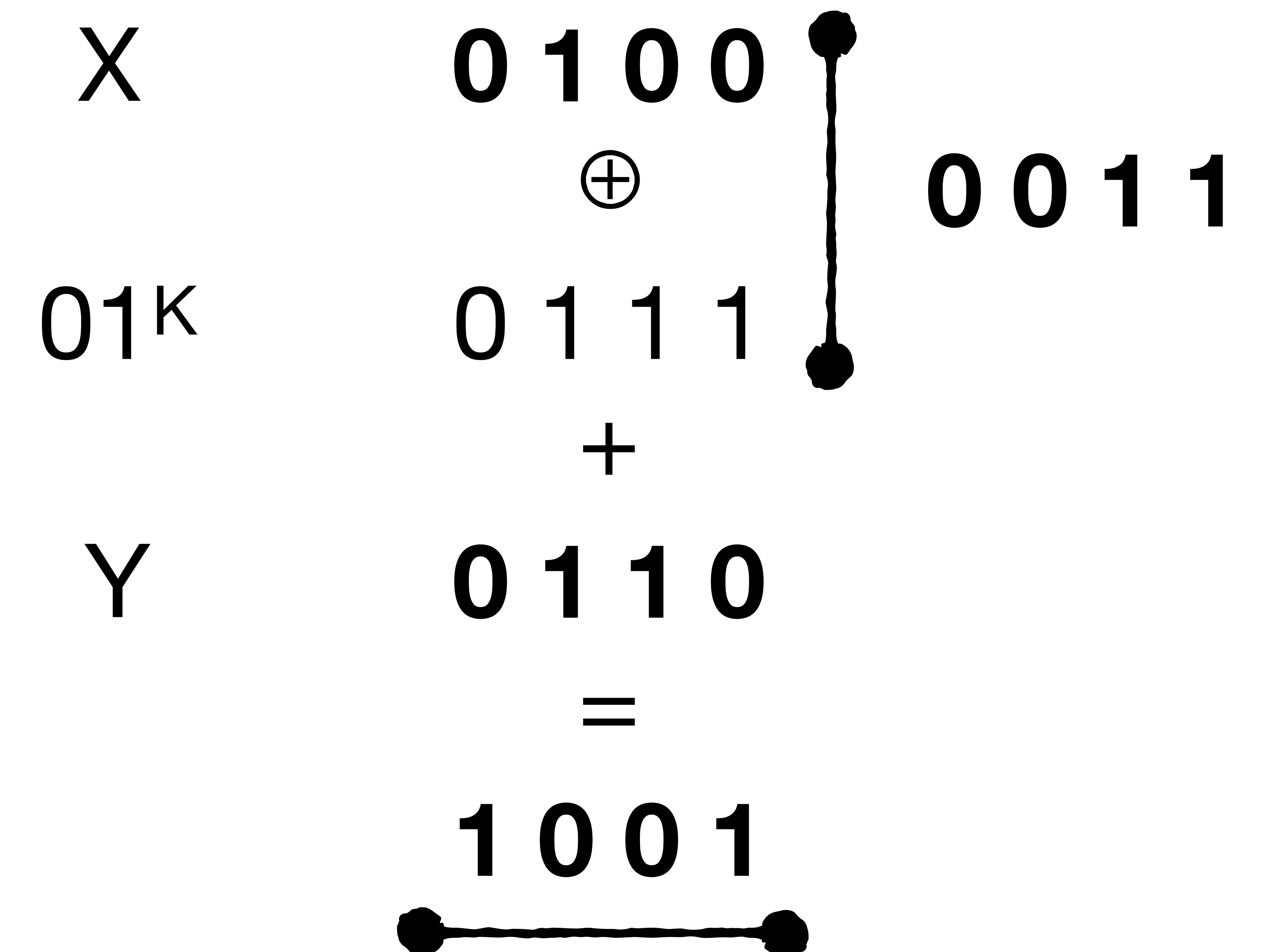


If X>Y, result decreases

How about range predicates?

Select * where X < Y

$X = Y$ iff $(X \oplus 01^K) + Y = 01^K$

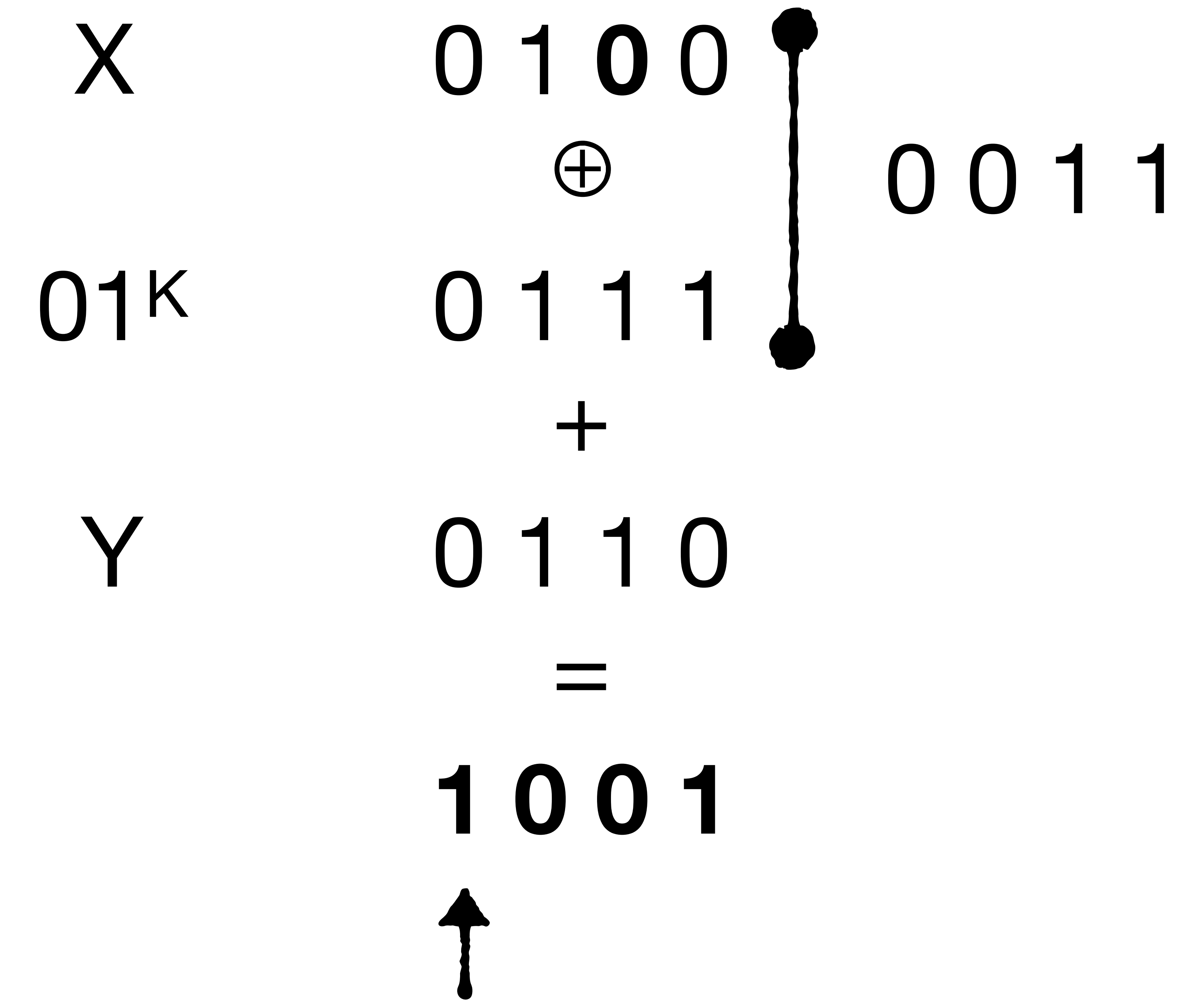


If X<Y, result increases

How about range predicates?

Select * where X < Y

$X = Y$ iff $(X \oplus 01^K) + Y = 01^K$

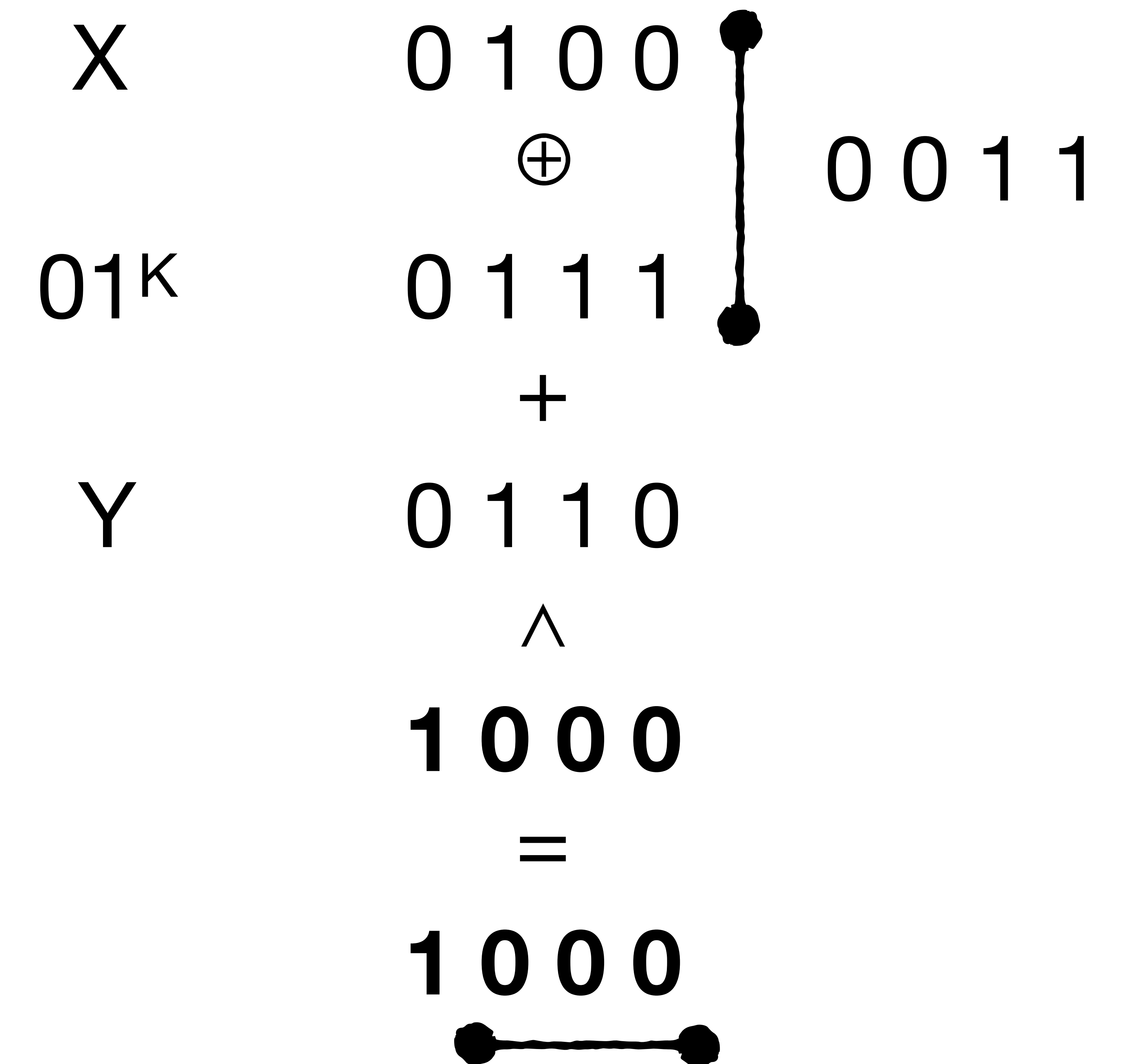


How about range predicates?

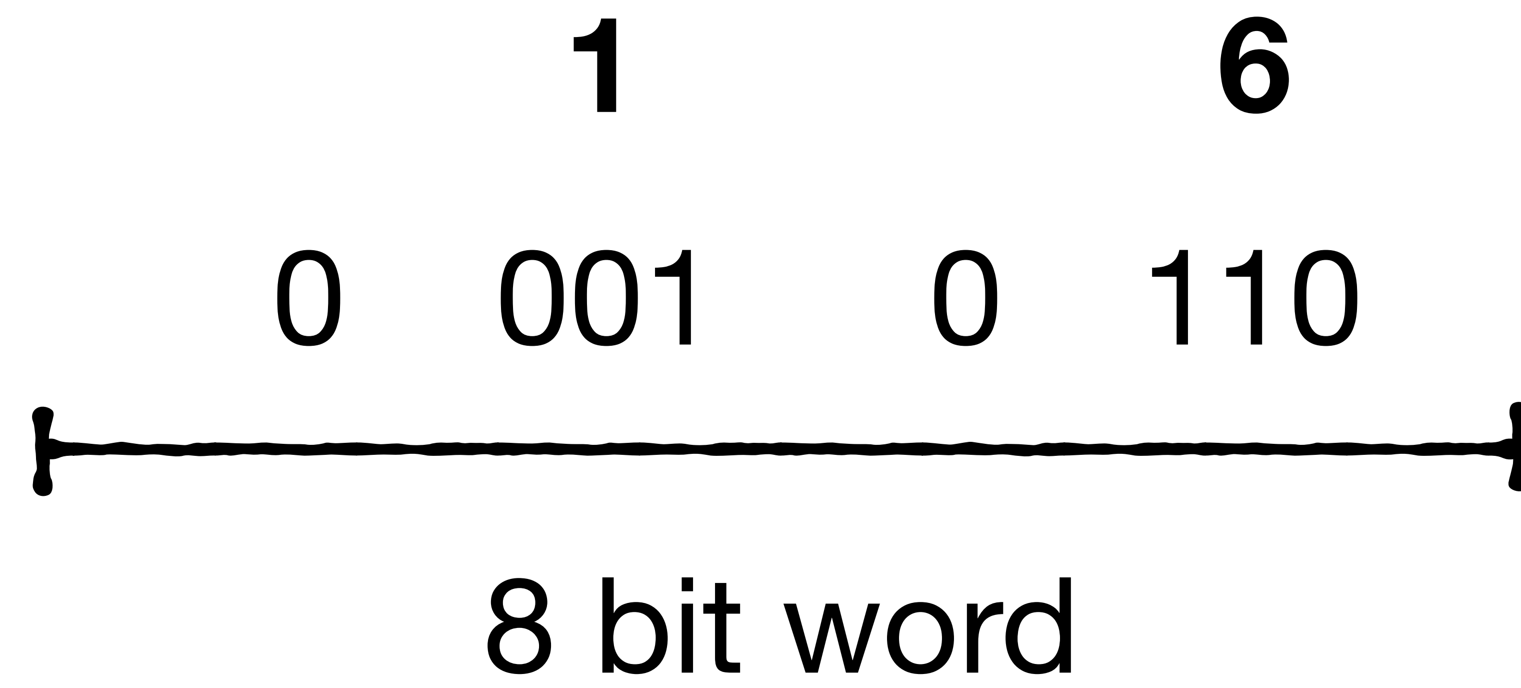
Select * where X < Y

$X = Y$ iff $(X \oplus 01^K) + Y = 01^K$

$X < Y$ iff $((X \oplus 01^K) + Y) \wedge 10^K = 10^K$

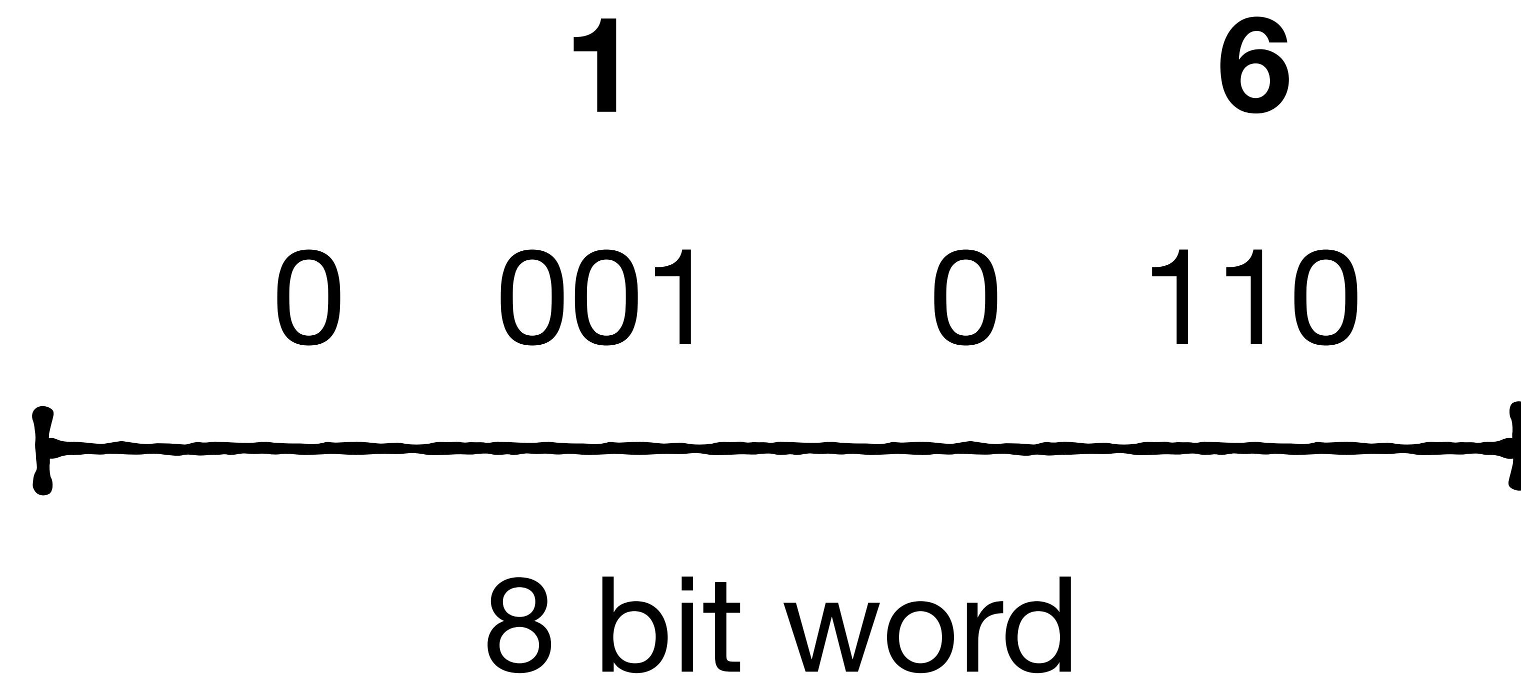


Now let's apply this in parallel on all codes in a word



Now let's apply this in parallel on all codes in a word

Select * where X < 5



Now let's apply this in parallel on all codes in a word

Select * where X < 5

word	0	001	0	110
		⊕		⊕
mask	**0**	**111**	**0**	**111**

Now let's apply this in parallel on all codes in a word

Select * where X < 5

word	0	001	0	110
		⊕		⊕
mask	0	111	0	111
		+		+
Constant	**0**	**101**	**0**	**101**

Now let's apply this in parallel on all codes in a word

Select * where X < 5

word	0	001	0	110
		⊕		⊕
mask	0	111	0	111
		+		+
Constant	0	101	0	101
		∧		∧
-mask	**1**	**000**	**1**	**000**

Now let's apply this in parallel on all codes in a word

Select * where X < 5

word $\oplus$ mask	0	**110**	0	**001**
		+		+
Constant	0	101	0	101
		$\wedge$		$\wedge$
-mask	1	000	1	000

Now let’s apply this in parallel on all codes in a word

Select * where X < 5

Constant + word ⊕ mask	1	**011**	0	**110**
		^		^
-mask	1	000	1	000

Now let’s apply this in parallel on all codes in a word

Select * where X < 5

$$(\text{Constant} + \text{word} \oplus \text{mask}) \wedge -\text{mask} = \mathbf{1}\quad 000\quad \mathbf{0}\quad 000$$

Next challenge: reducing sparse result vector into bitmap

1 000 **0** 000 → **1 0**

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1 000 **0** 000 → **1 0**

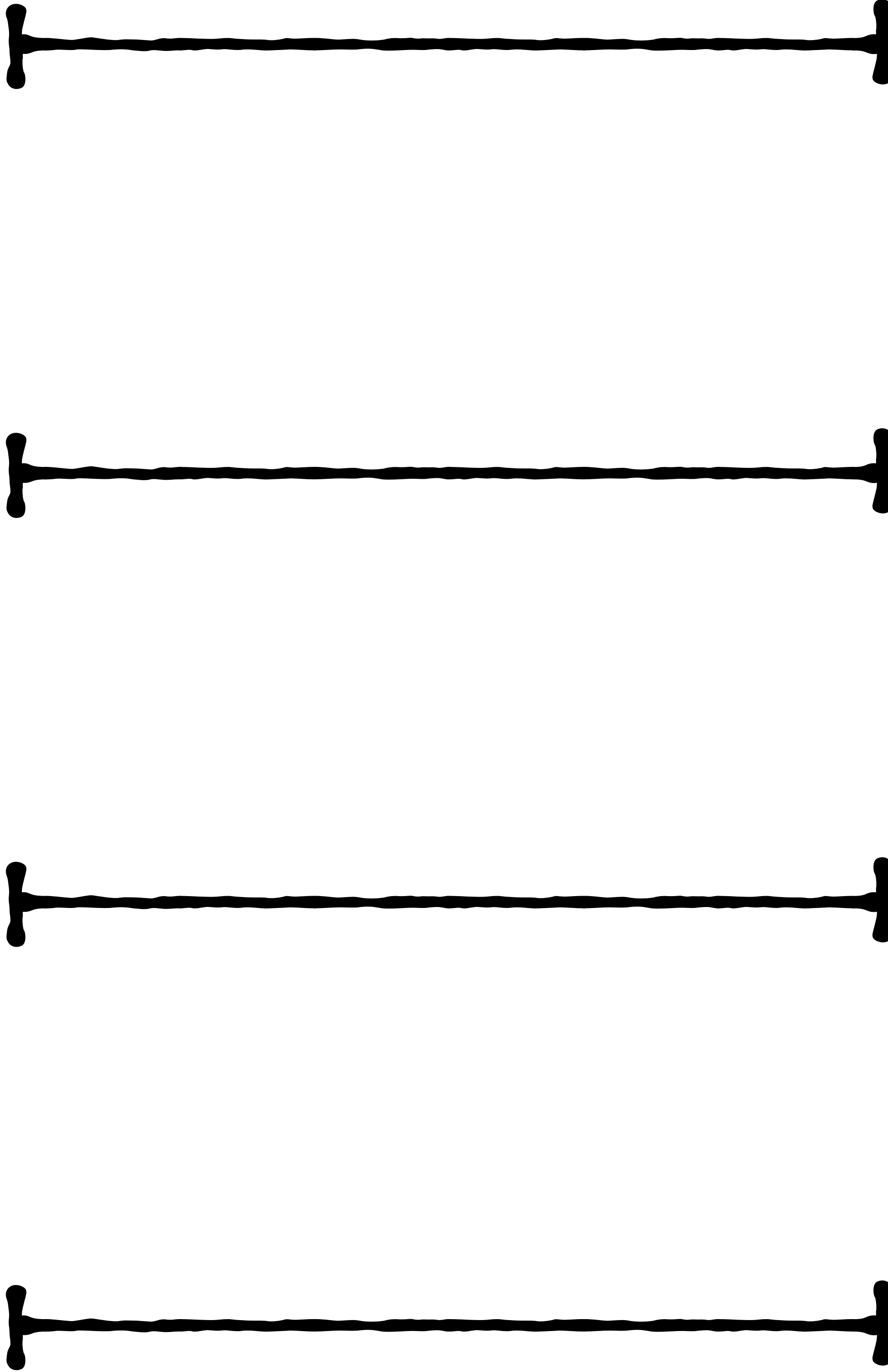
Bit Shifting
(From paper)

Parallel Bit Extract - PEXT
(Intel Haswell BMI2, 2013)

Bit Shifting

Column codes

c1 001
c2 101
c3 110
c4 001
c5 110
c6 100
c7 000
c8 111



1

2

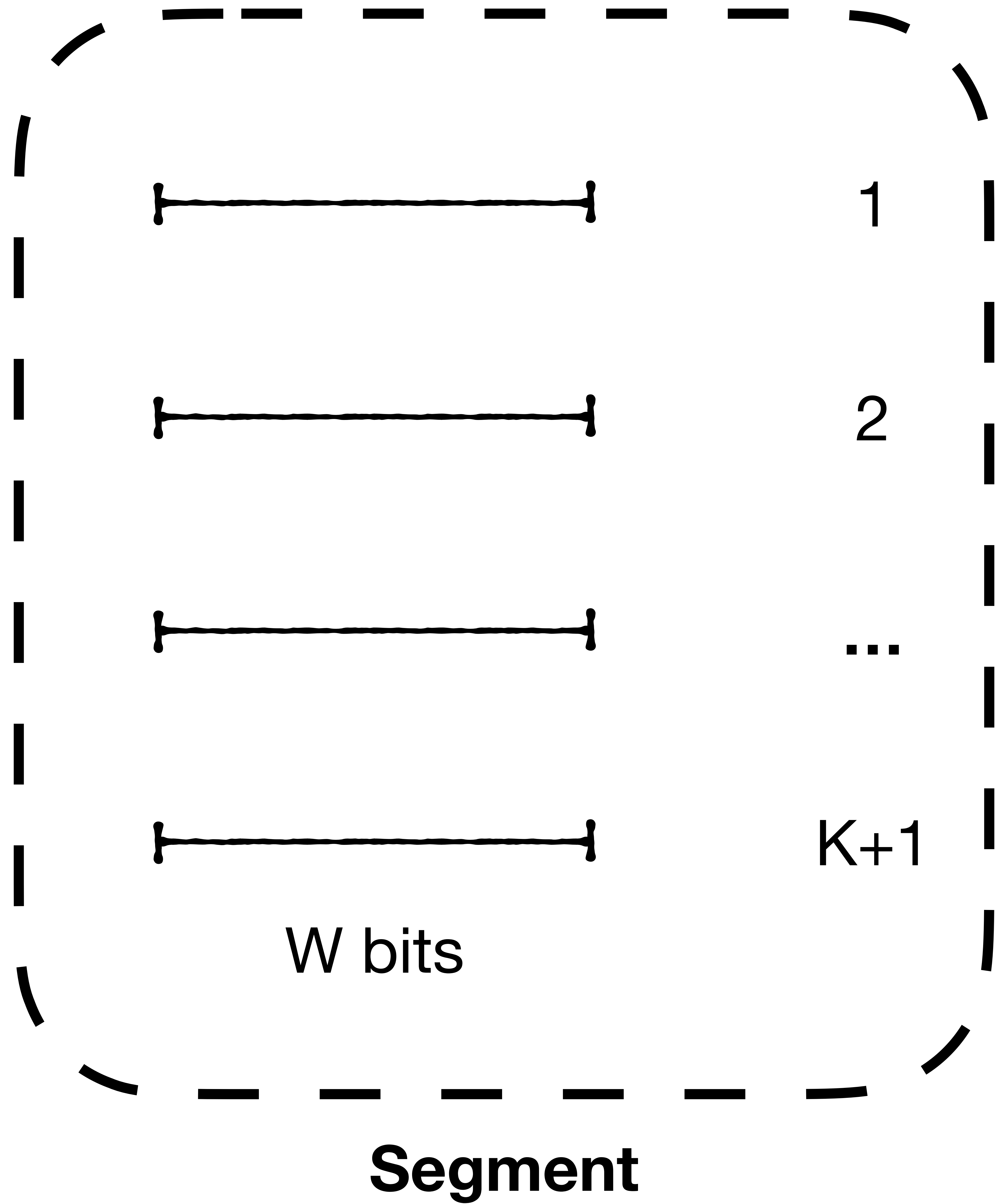
...

K+1

W bits

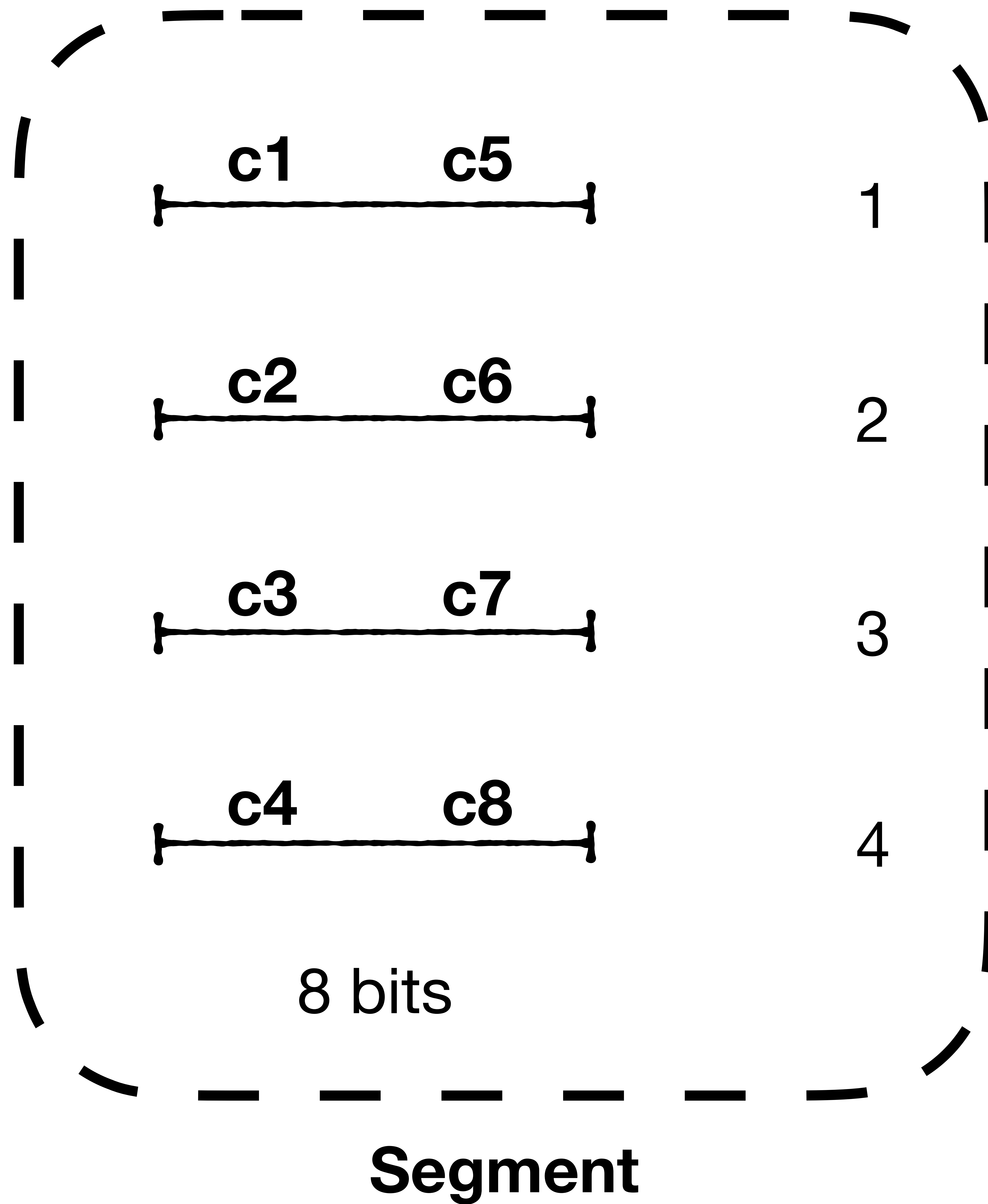
Column codes

c1	001
c2	101
c3	110
c4	001
c5	110
c6	100
c7	000
c8	111

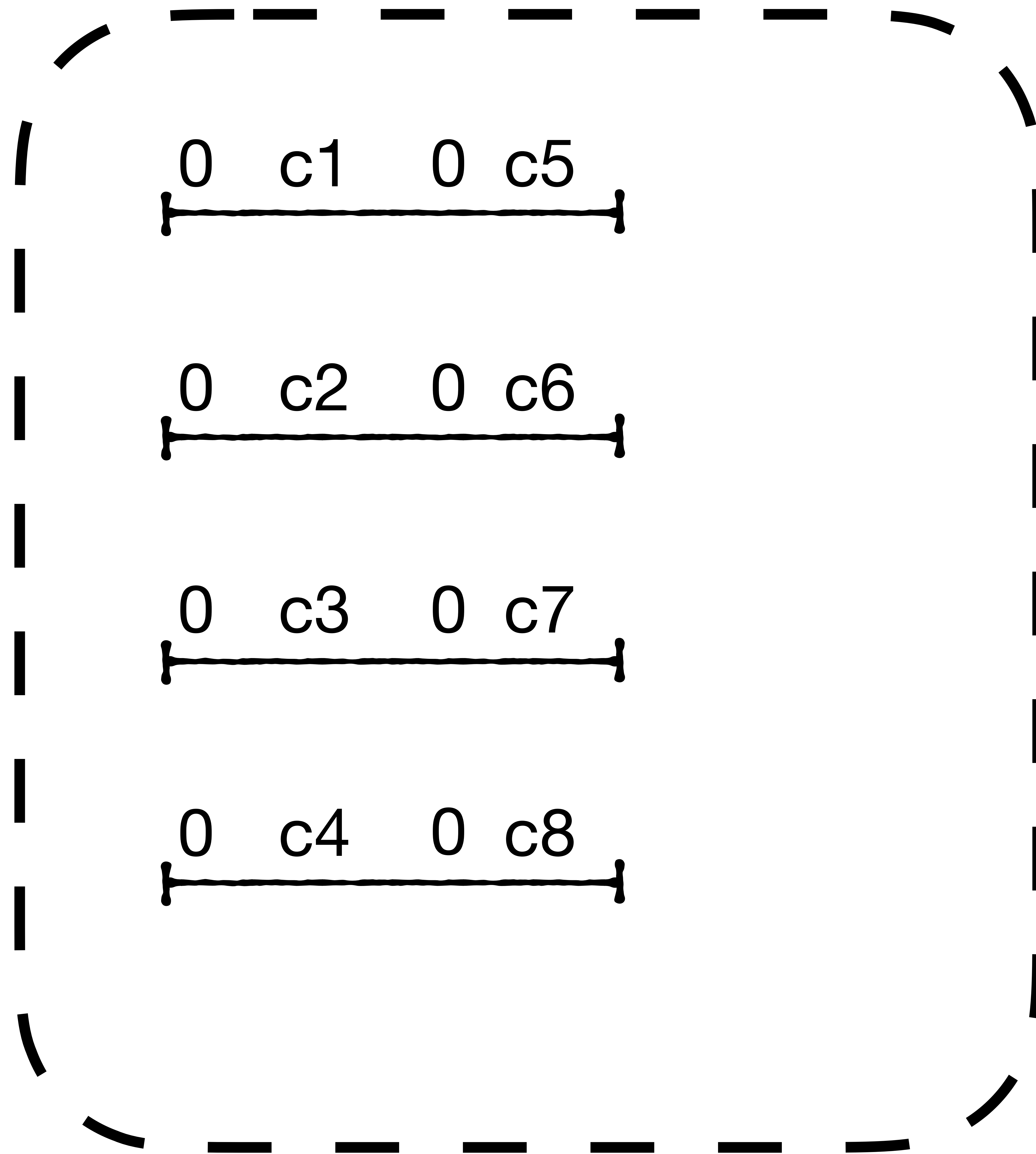


Column codes

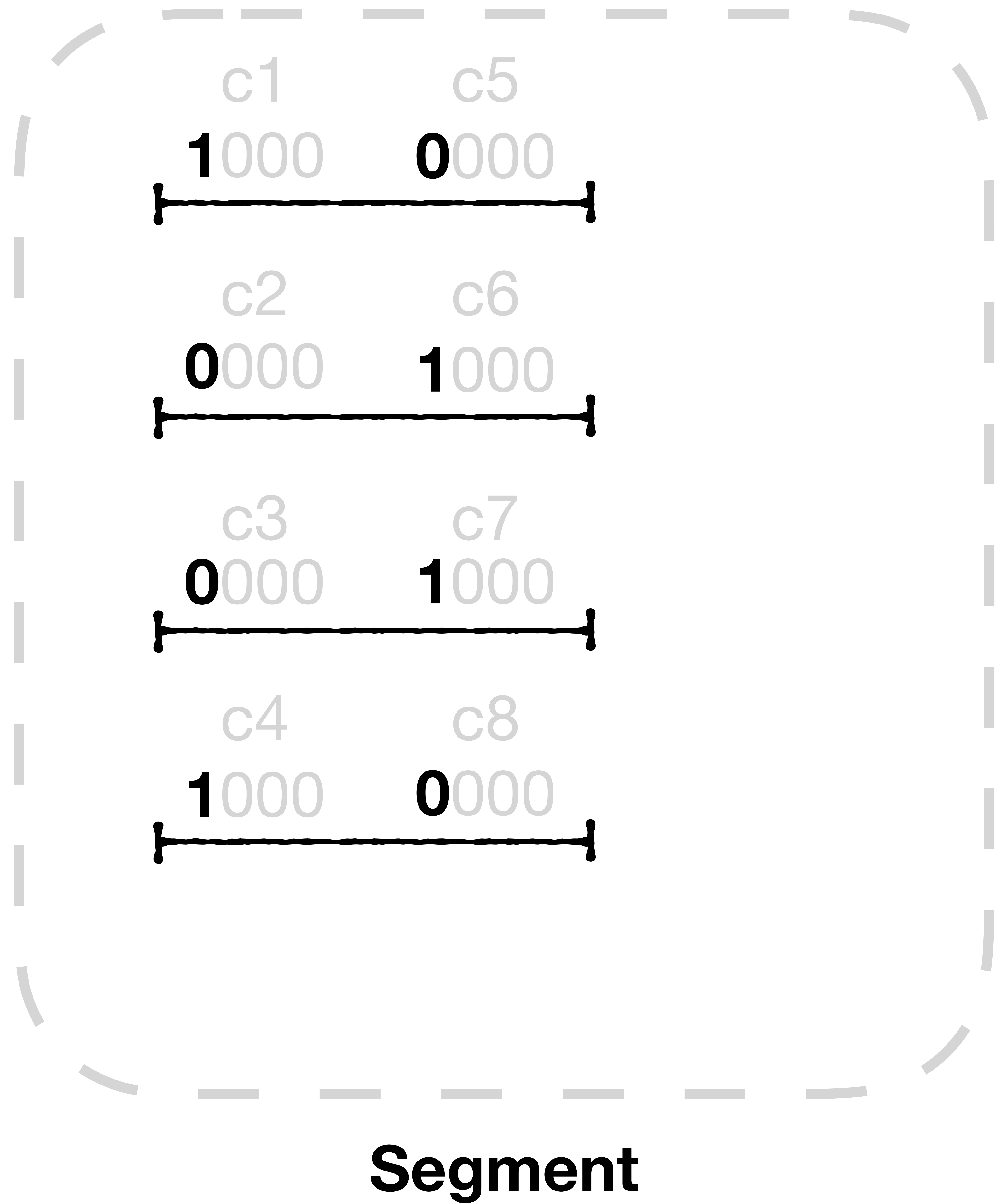
c1	001
c2	101
c3	110
c4	001
c5	110
c6	100
c7	000
c8	111



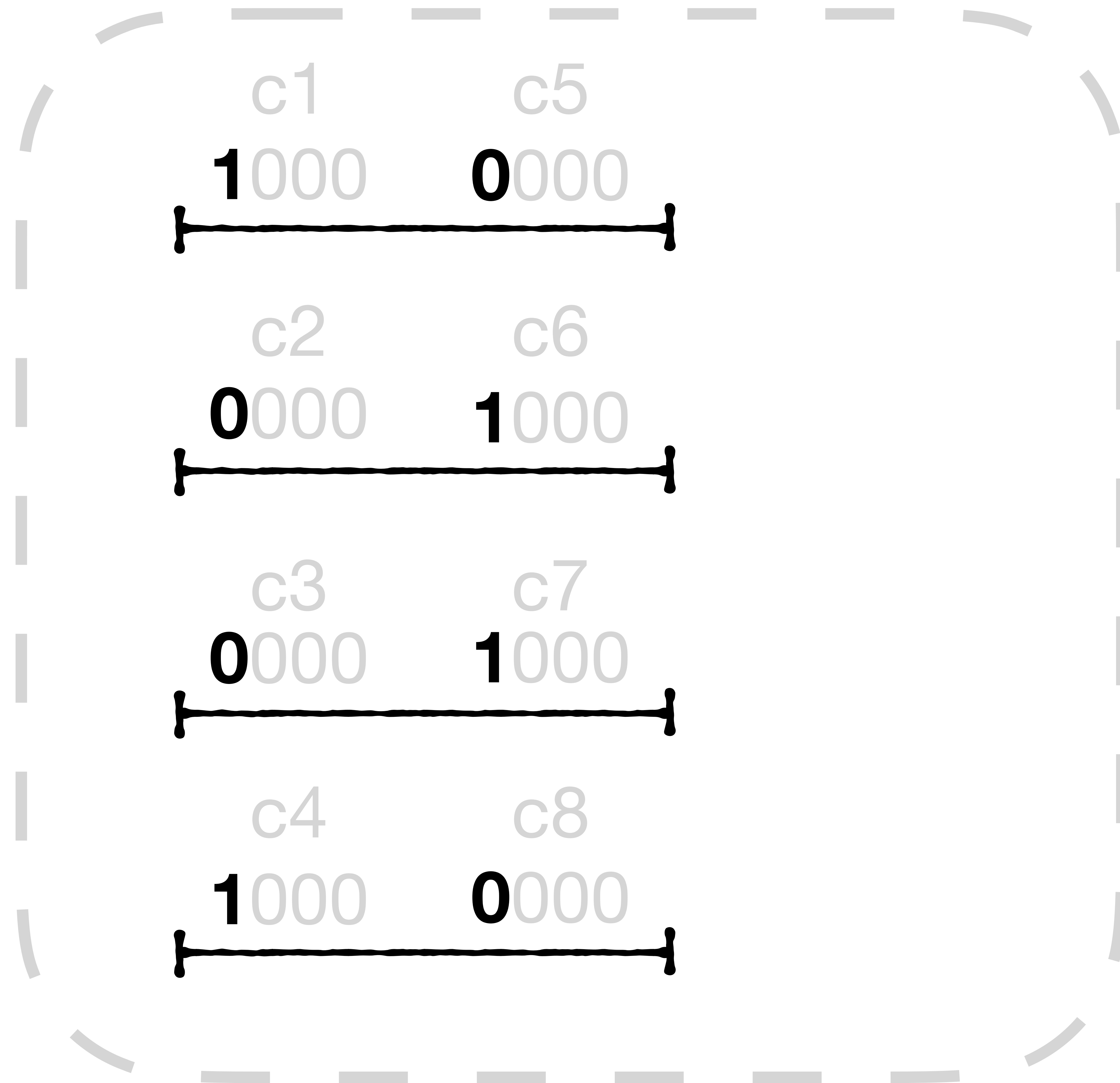
Add delimiter / result bit



Suppose we run a query



Suppose we run a query

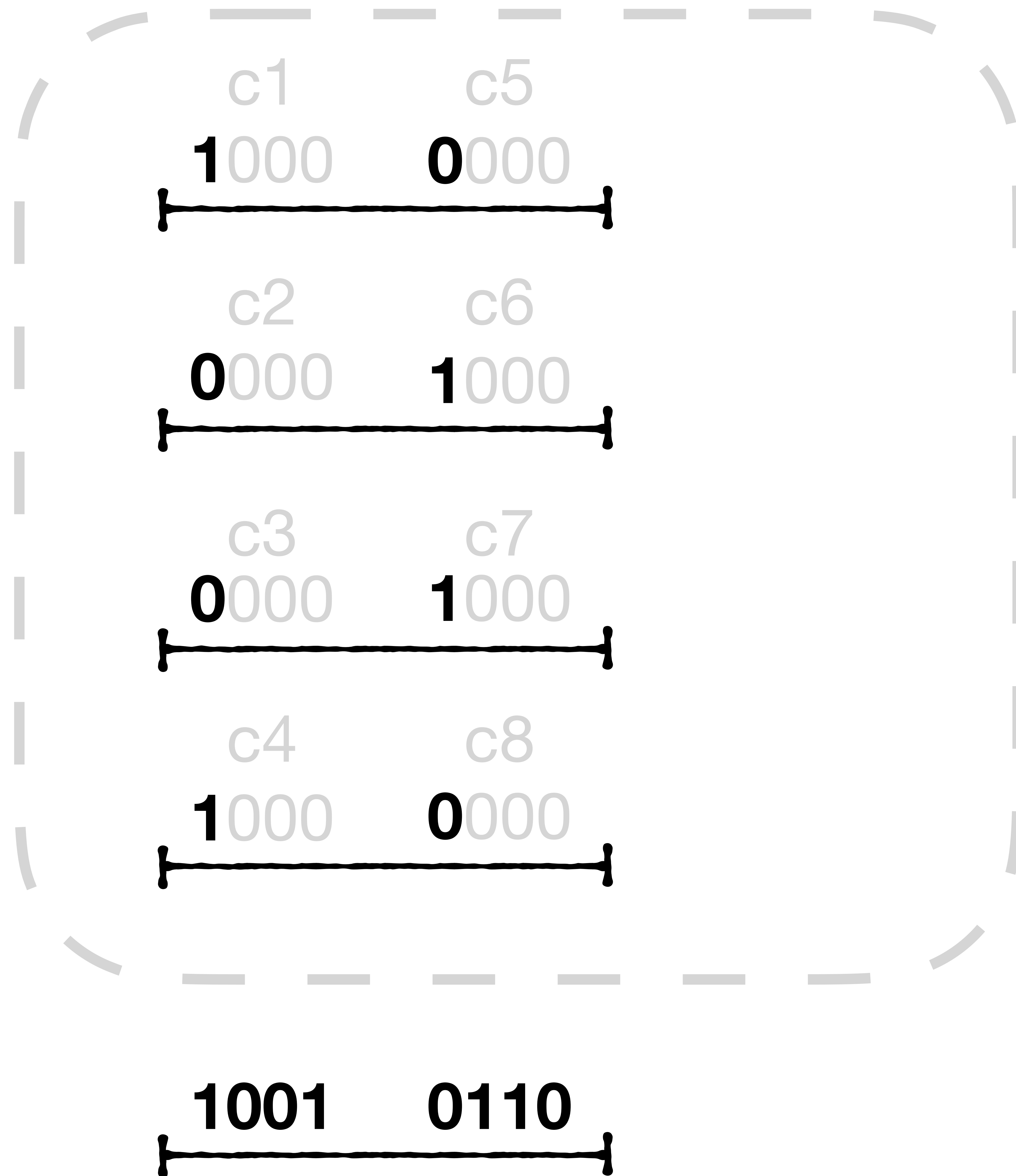


Expected result: 1001 0110

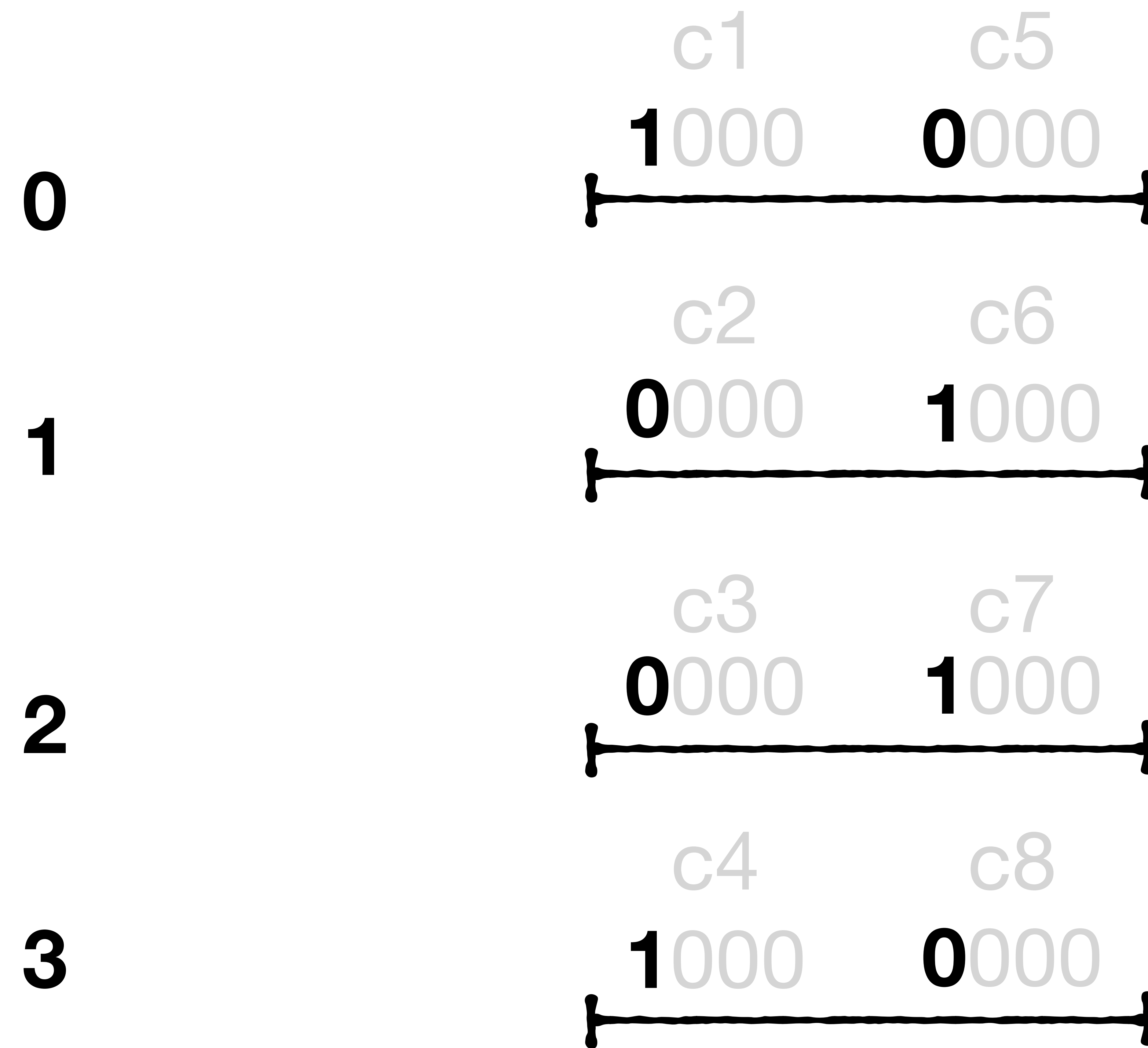
Suppose we run a query

What shifts do we do?

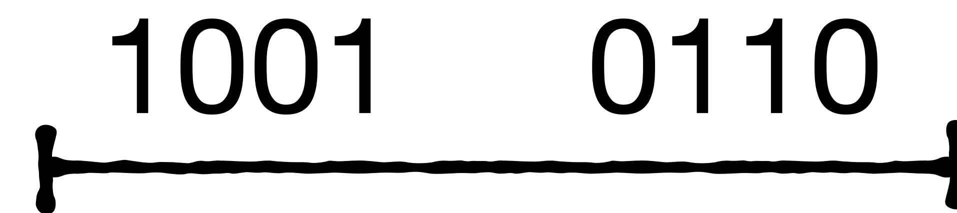
Expected result:



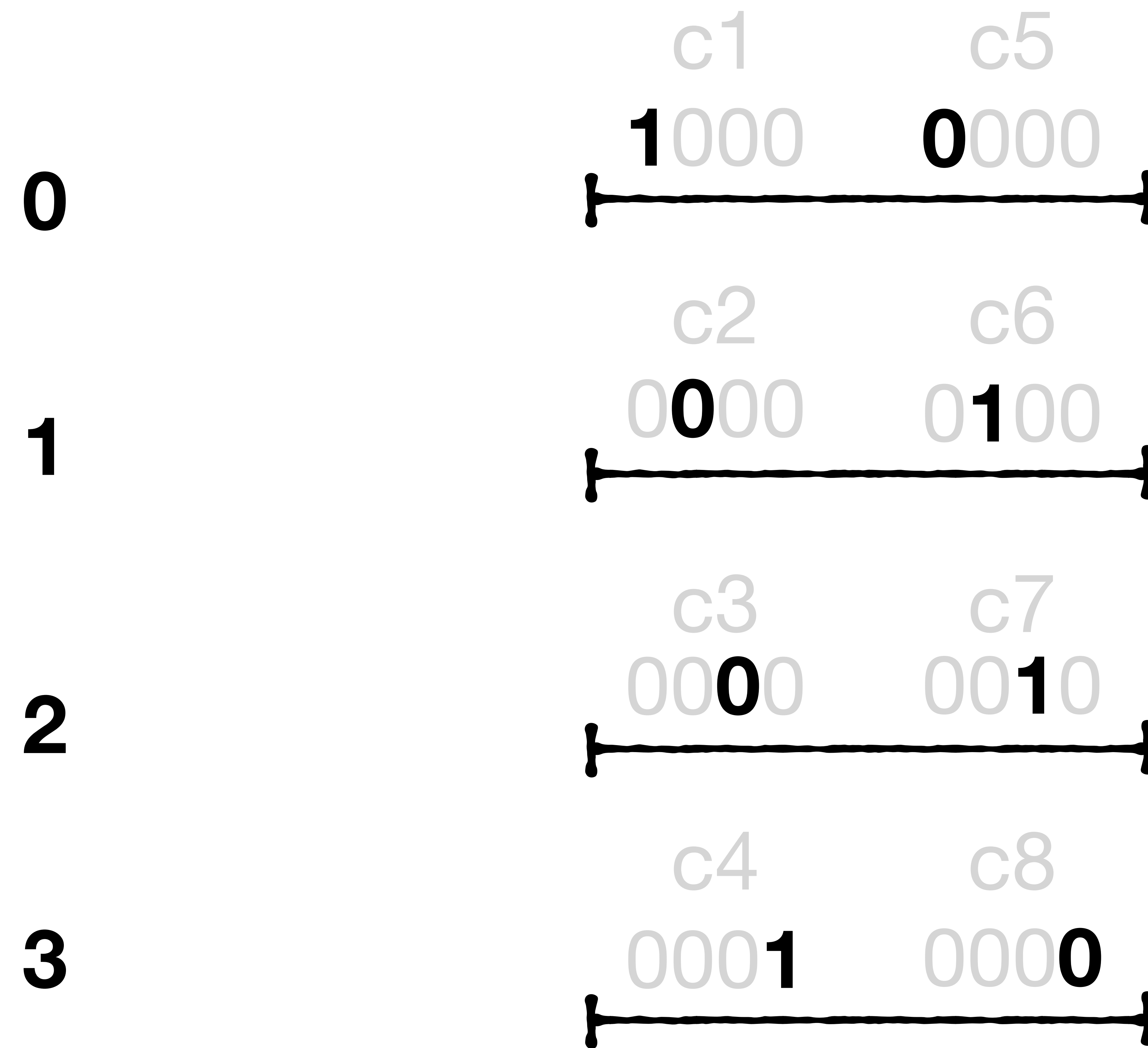
Rightwards bit shift



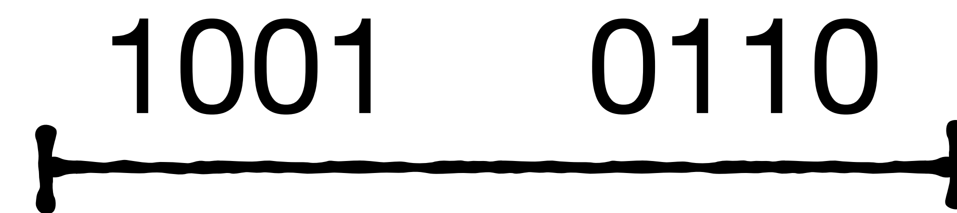
Expected result:

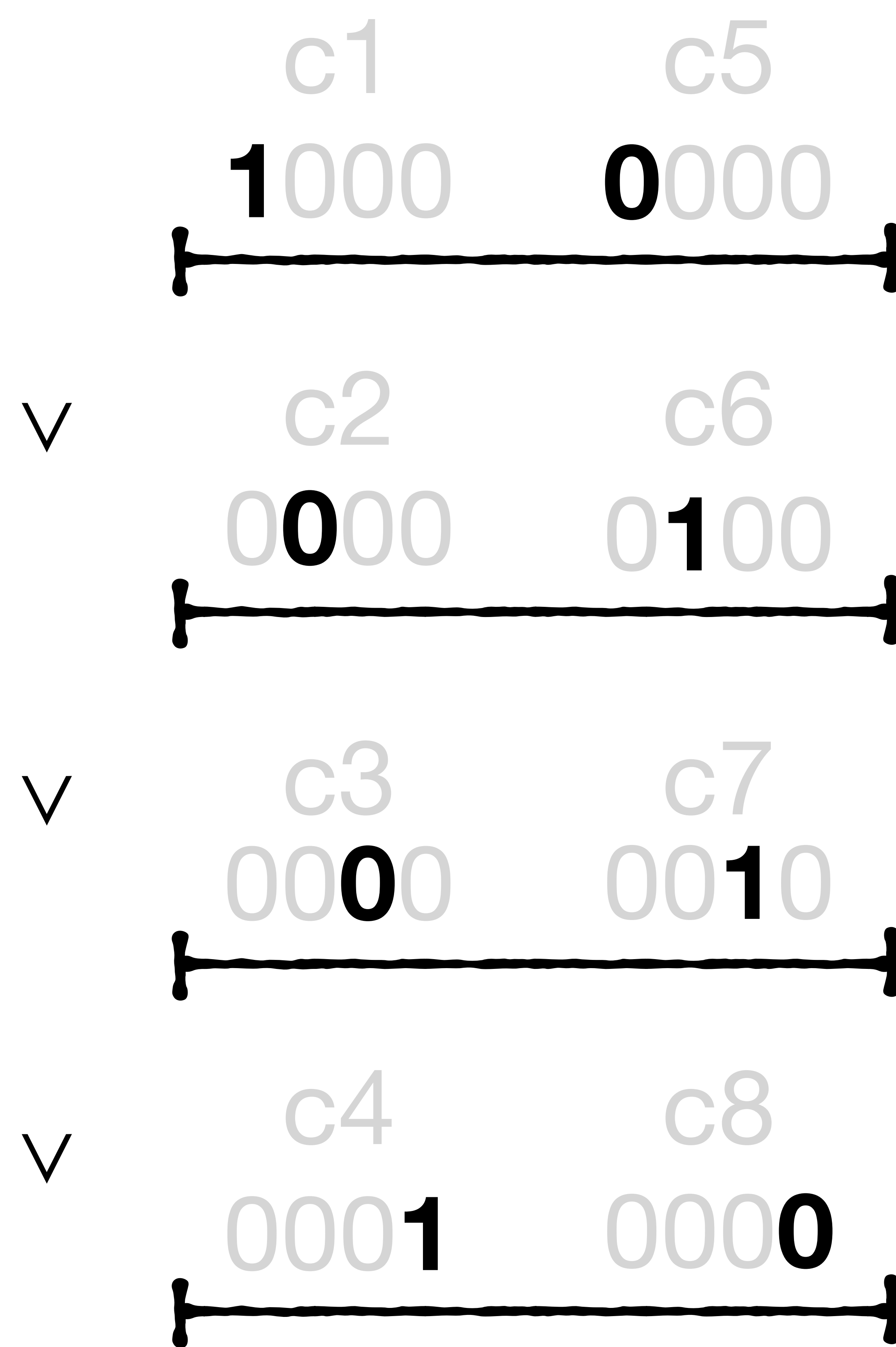


Rightwards bit shift



Expected result:





Now "or" all the words into result:

Bit Shifting
(From paper)

Parallel Bit Extract - PEXT
(Intel Haswell BMI2, 2013)

Parallel Bit Extract - PEXT

Extract bits at specific locations and store them contiguously

Parallel Bit Extract - PEXT

Extract bits at specific locations and store them contiguously

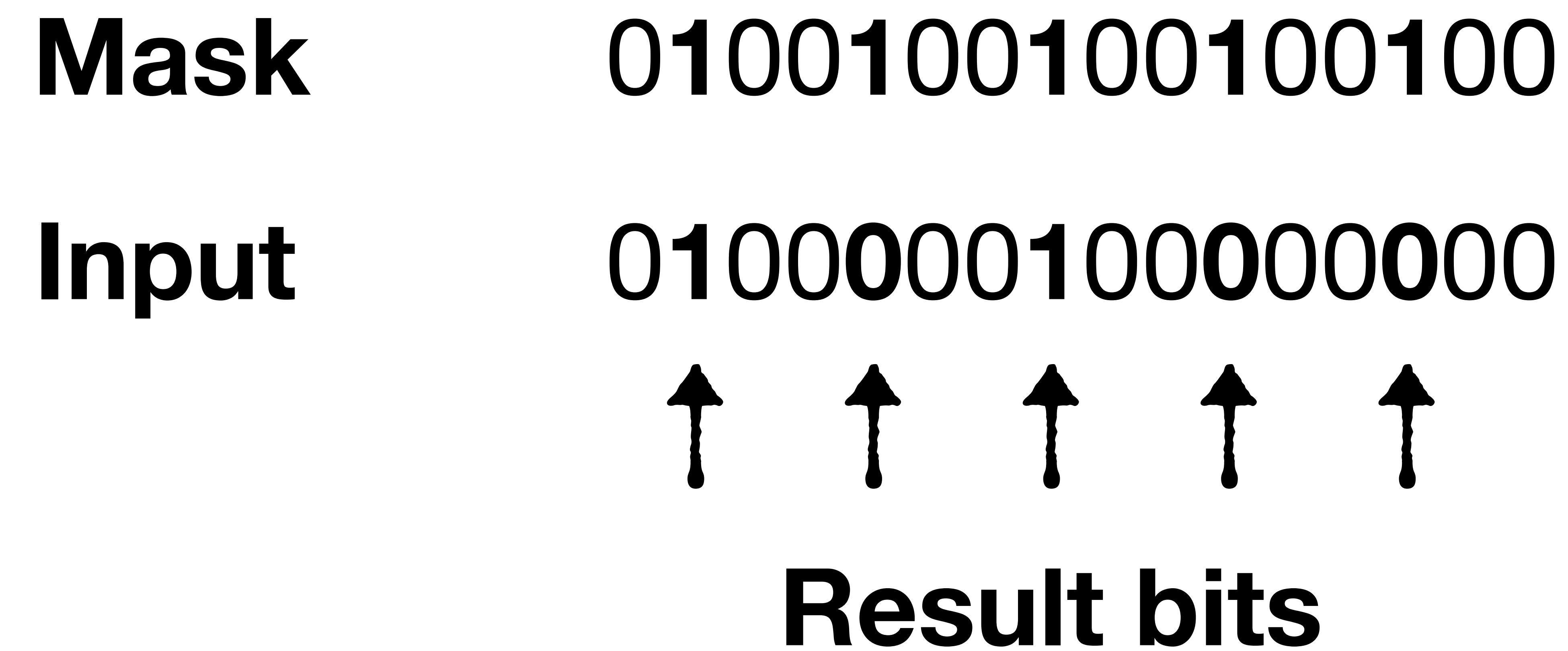
Mask 0**1**00**1**00**1**00**1**00**1**00

Input 0**1**00**0**00**1**00**0**00**0**00

E.g., 2 bit codes, 16 bit register

Parallel Bit Extract - PEXT

Extract bits at specific locations and store them contiguously



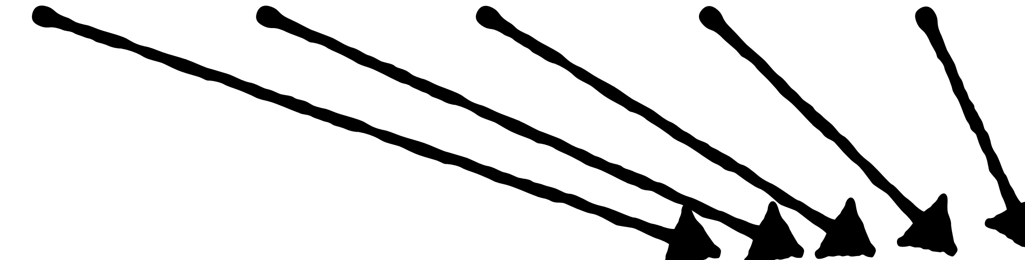
E.g., 2 bit codes, 16 bit register

Parallel Bit Extract - PEXT

Extract bits at specific locations and store them contiguously

Mask 0**1**00**1**00**1**00**1**00**1**00

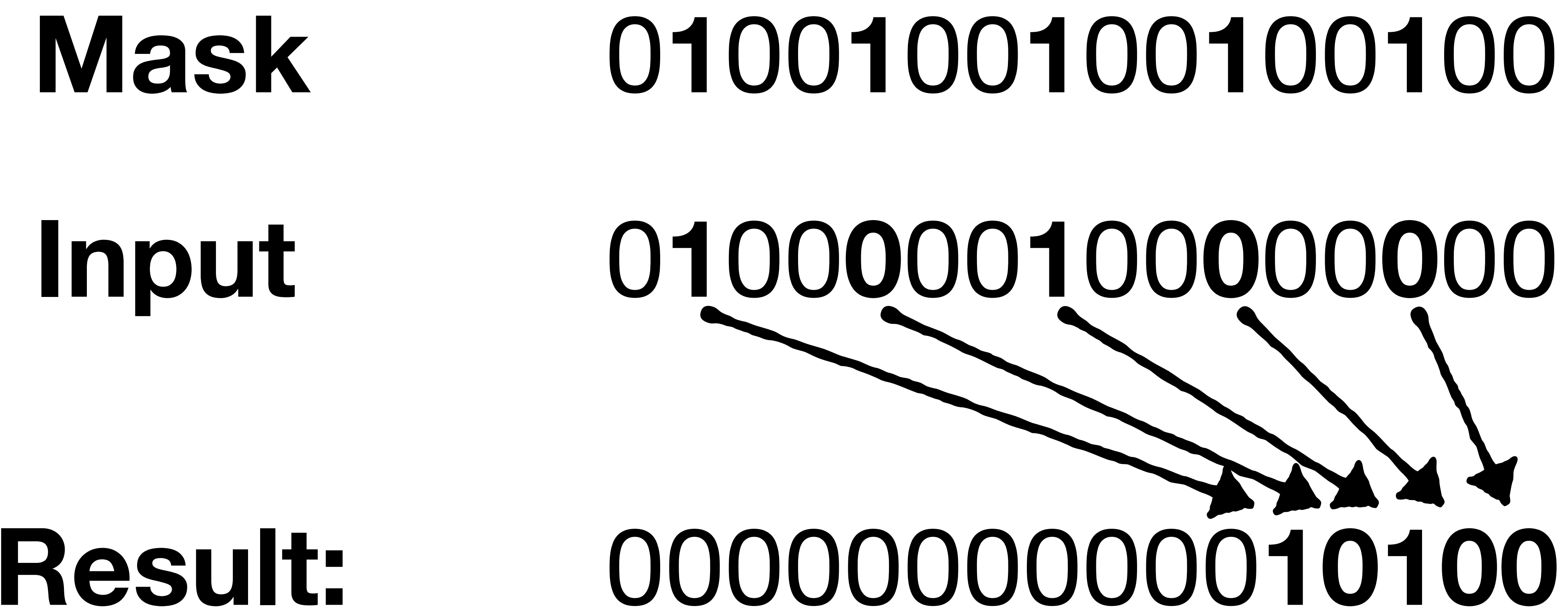
Input 0**1**00**0**00**1**00**0**00**0**00



Result: 00000000000**10100**

Parallel Bit Extract - PEXT

Extract bits at specific locations and store them contiguously



Counterpart to PDEP

(from lecture on quotient filters)

Horizontal BitWeaving Summary

Packs codes efficiently into word

Uses word-level parallelism

Does not do early pruning

Some padding at end

BitWeaving: Fast Scans for Main Memory Data Processing

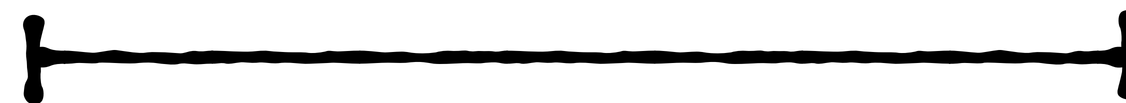
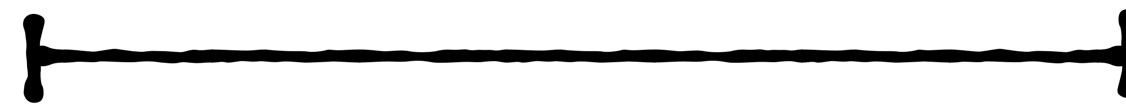
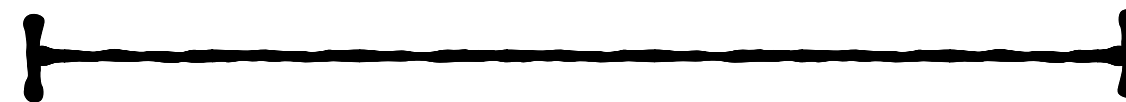
Horizontal

Vertical

Vertical BitWeaving

Column codes

c1	001
c2	101

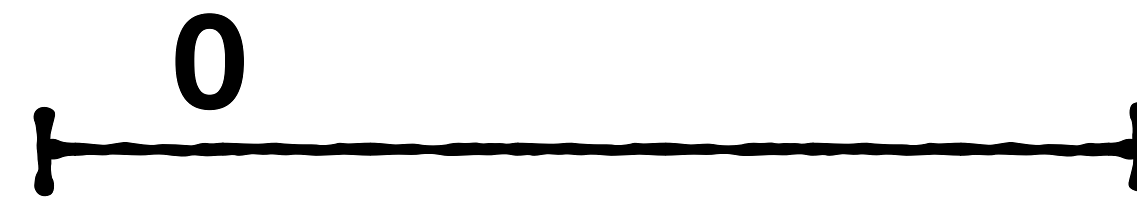




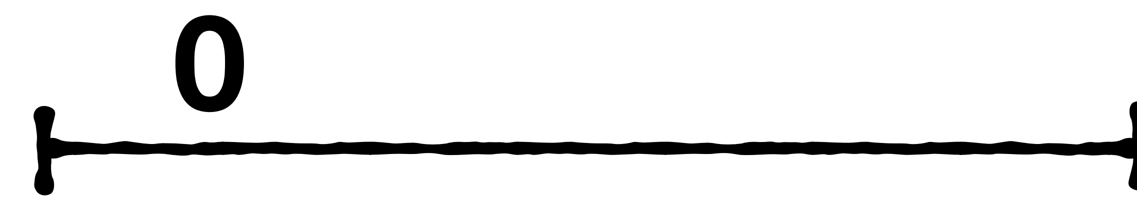
8 bit word

Vertical BitWeaving

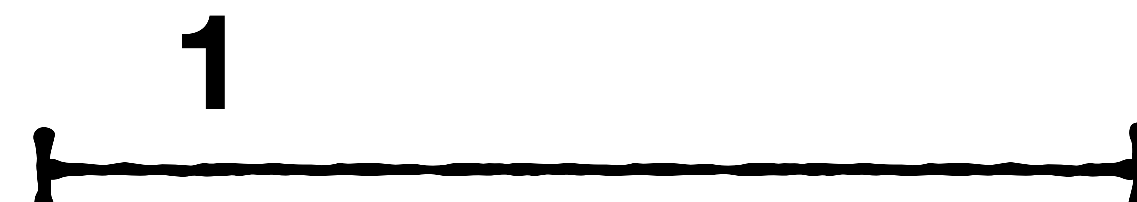
Column codes

c1	**001**
c2	101





8 bit words



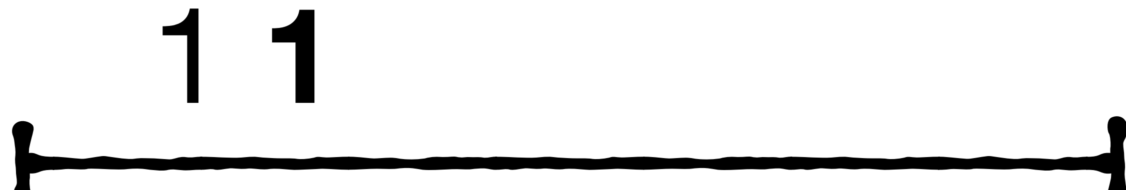
Column codes

c1	001
c2	**101**

0 **1**

0 **0**

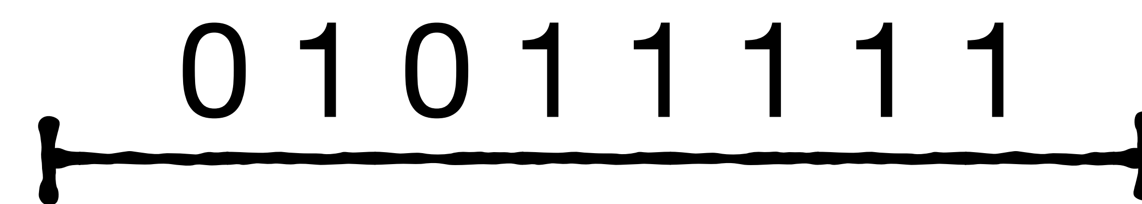
1 **1**

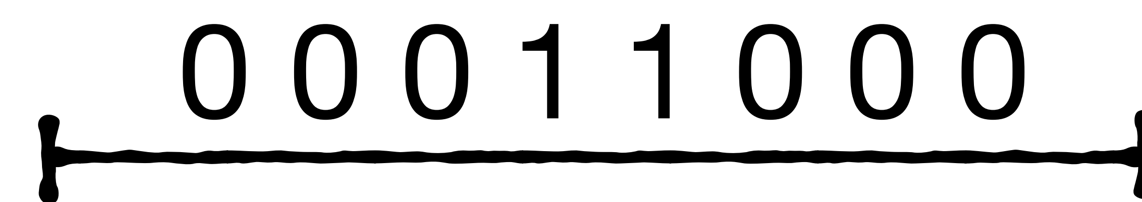


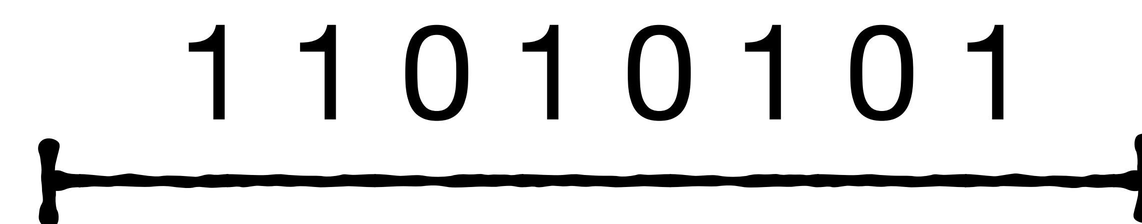
8 bit words

Column codes

c1	001
c2	101
c3	000
c4	111
c5	110
c6	101
c7	100
c8	101

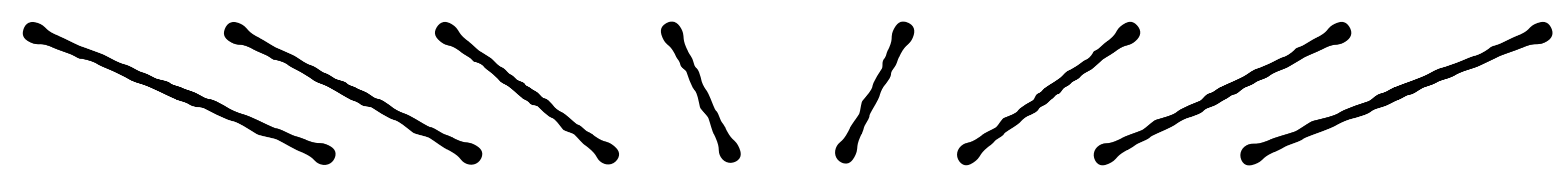






8 bit words

c1 c2 c3 c4 c5 c6 c7 c8

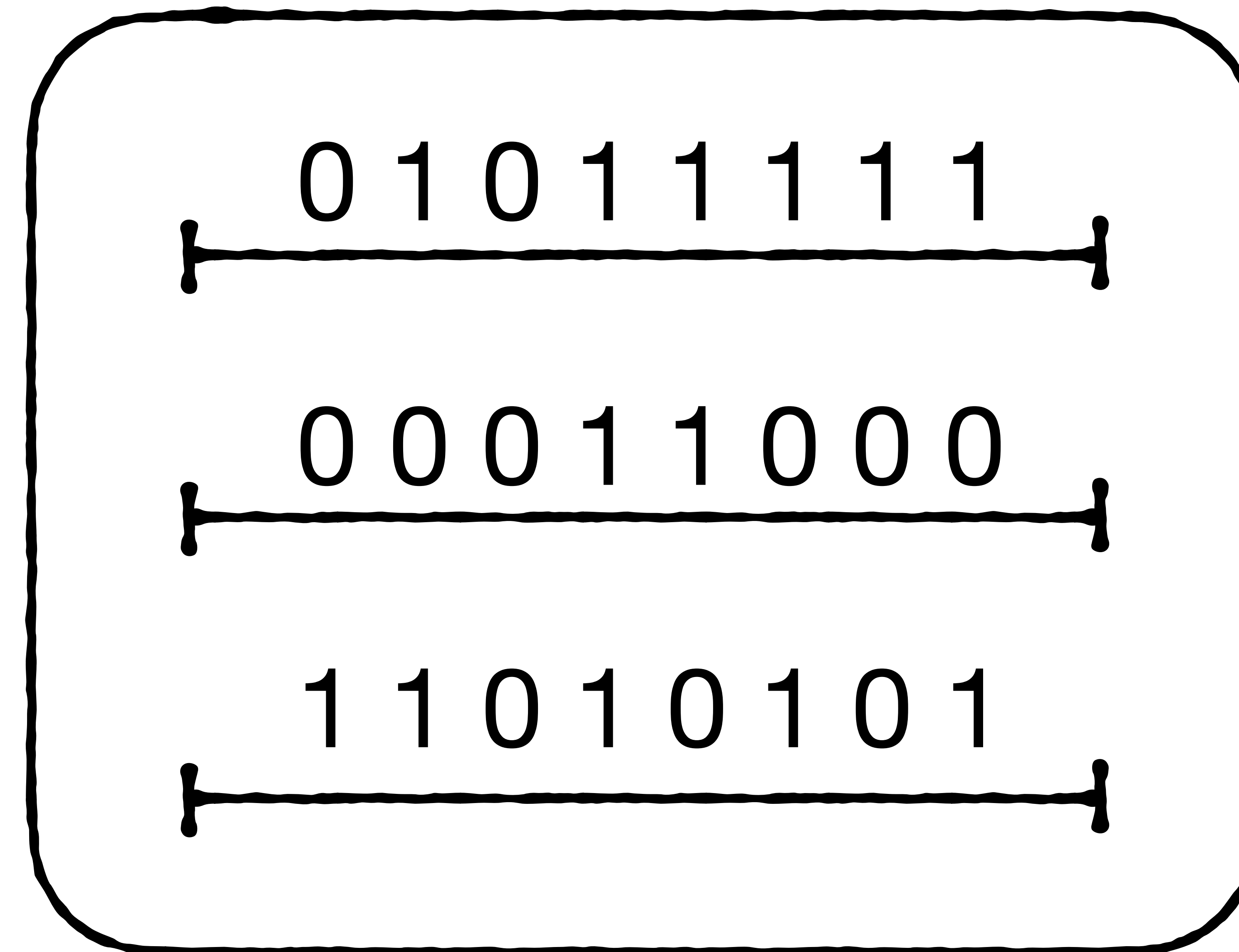


0 1 0 1 1 1 1 1

0 0 0 1 1 0 0 0

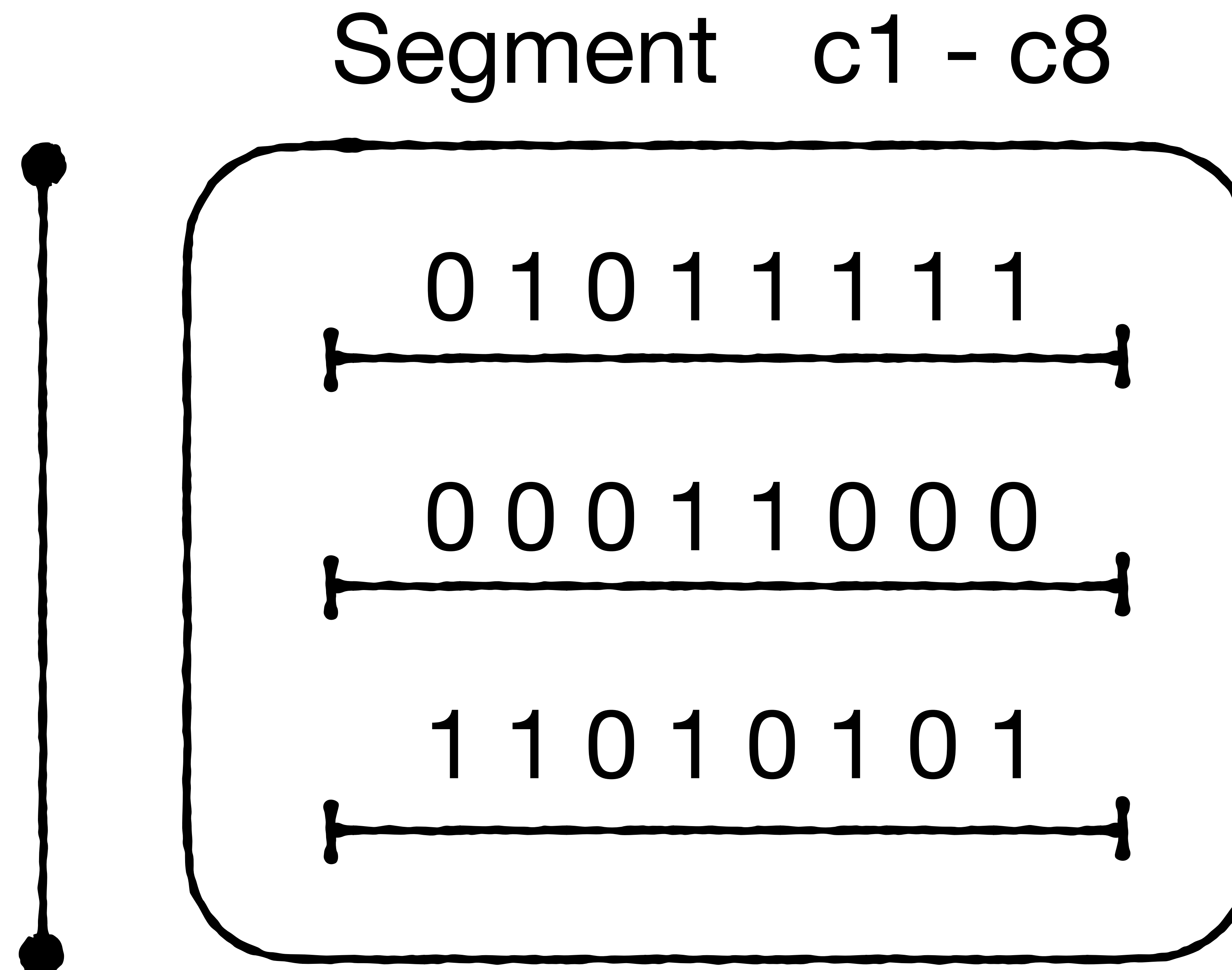
1 1 0 1 0 1 0 1

8 bit words


Segment c1 - c8
0 1 0 1 1 1 1 1
0 0 0 1 1 0 0 0
1 1 0 1 0 1 0 1

|C| words per segment, where |C| is code length

e.g., 3



|W| codes per segment, where |W| is word length

e.g., 8

Segment c1 - c8

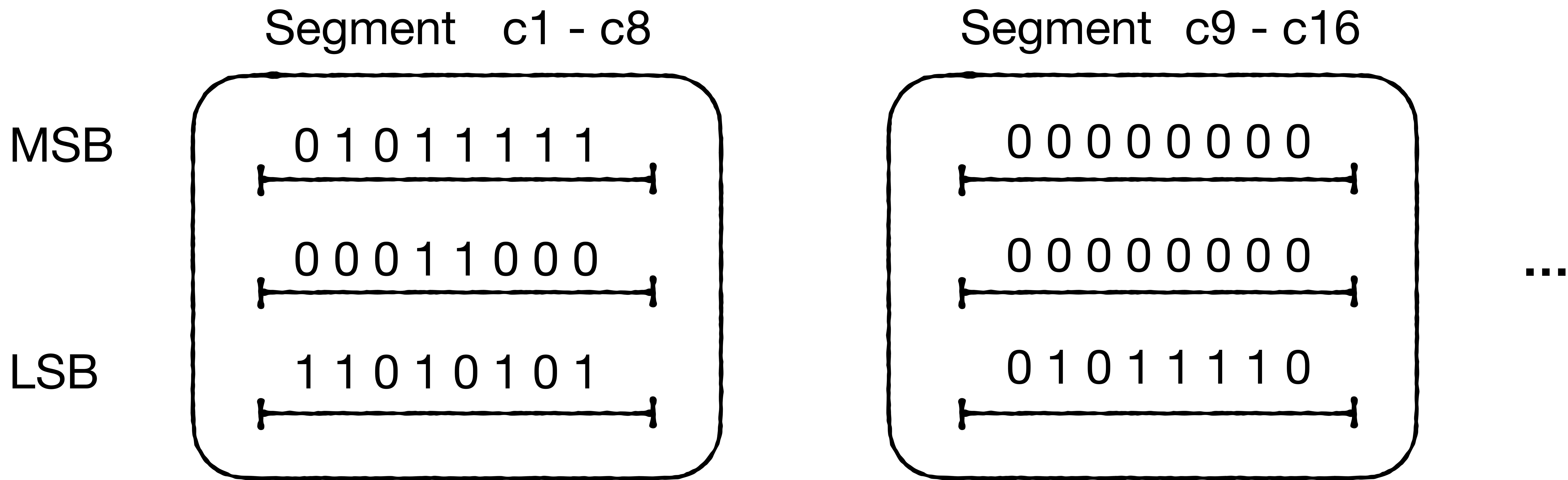
Segment c9 - c16

MSB

0 1 0 1 1 1 1 1

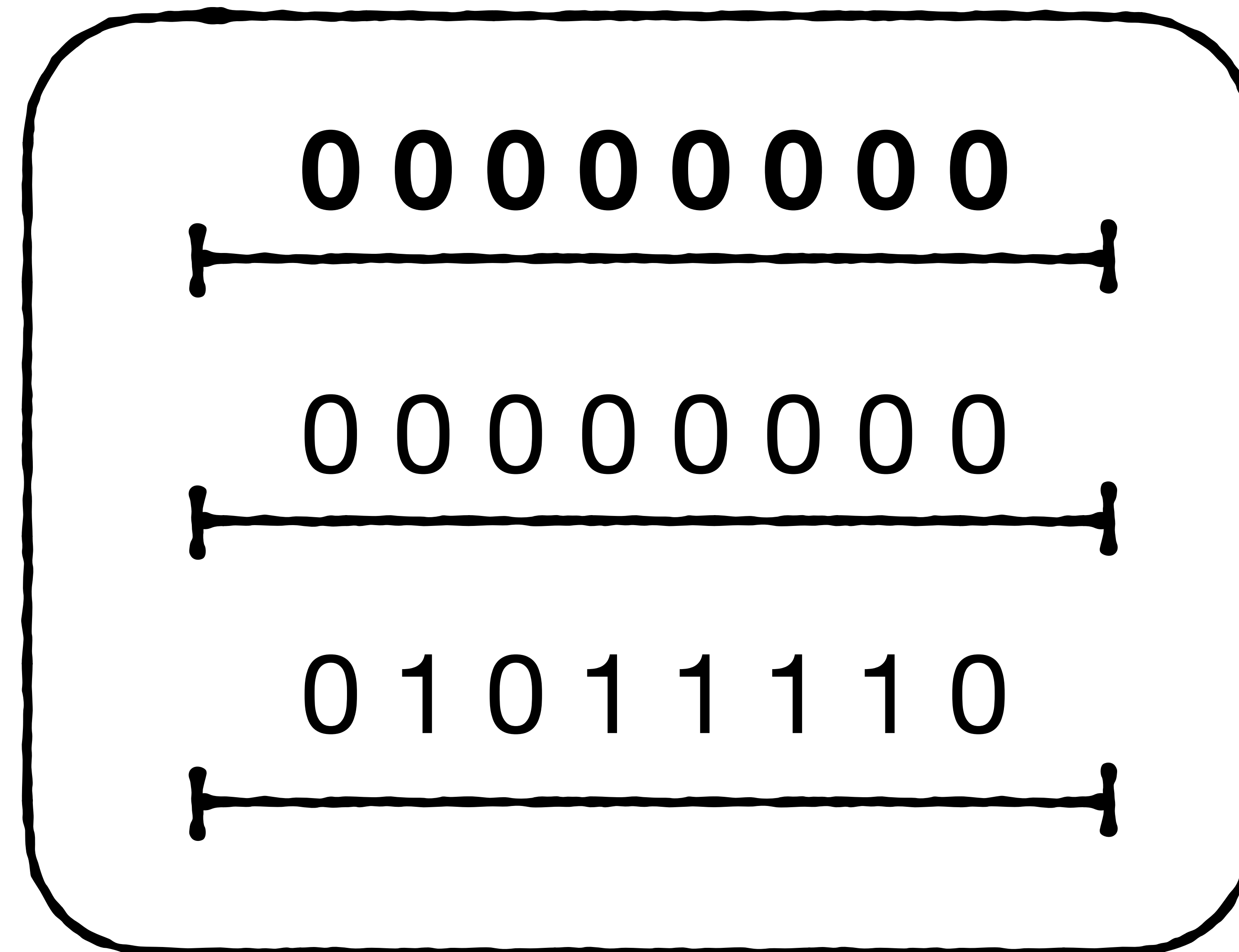
0 0 1 1 0 0 0 0 0 0 (row 2 below)

LSB



Select * where c > 100

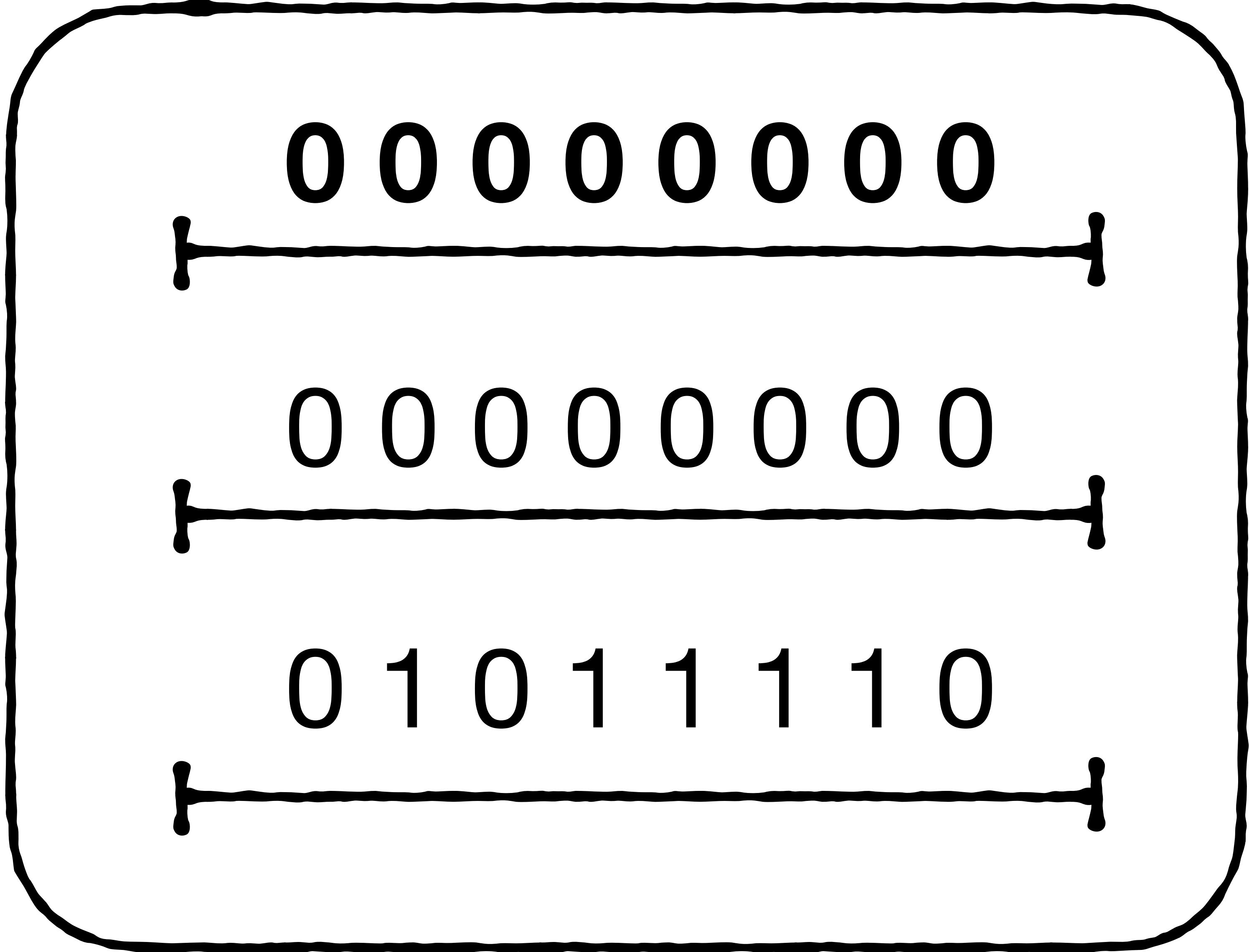
Segment c9 - c16



Check

Select * where c > 100

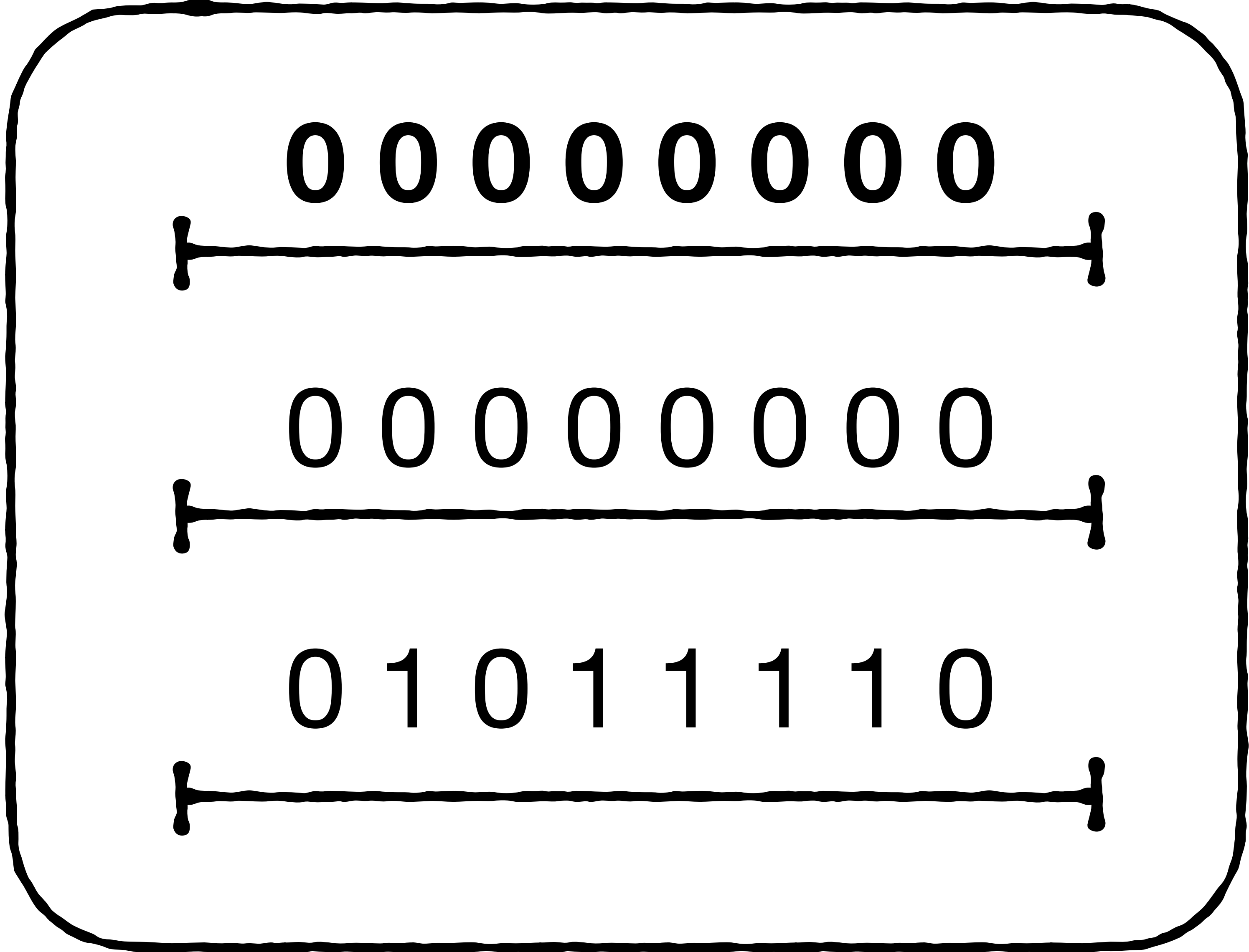
Segment c9 - c16

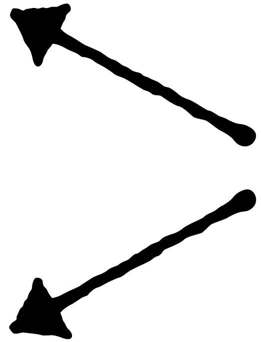


Check

No need to scan further :)

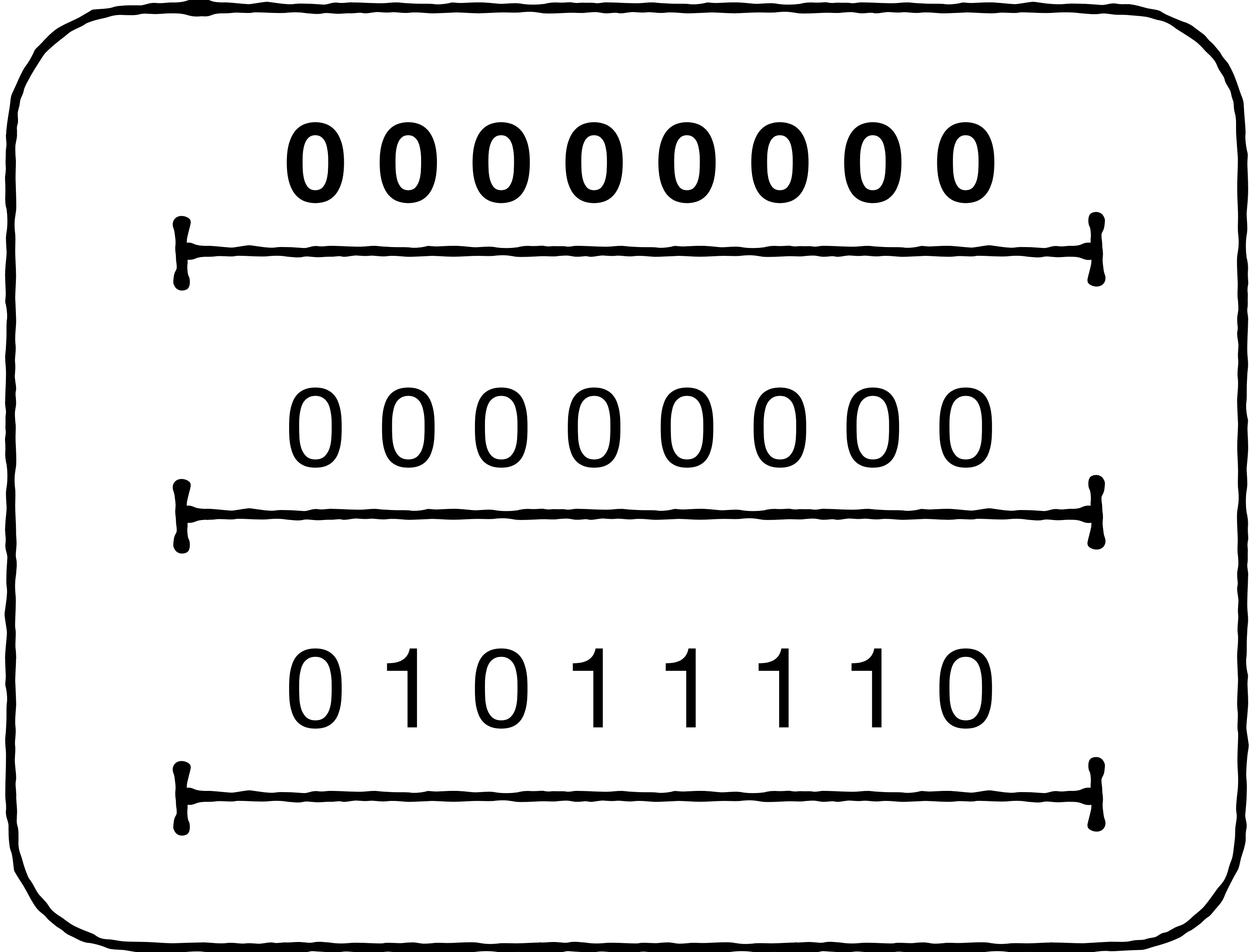
Select * where c > 100

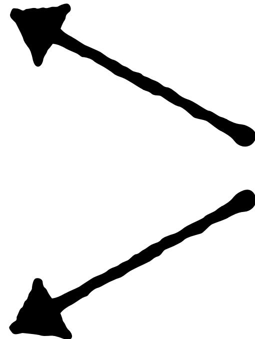




But these still pollute the cache

Select * where c > 100



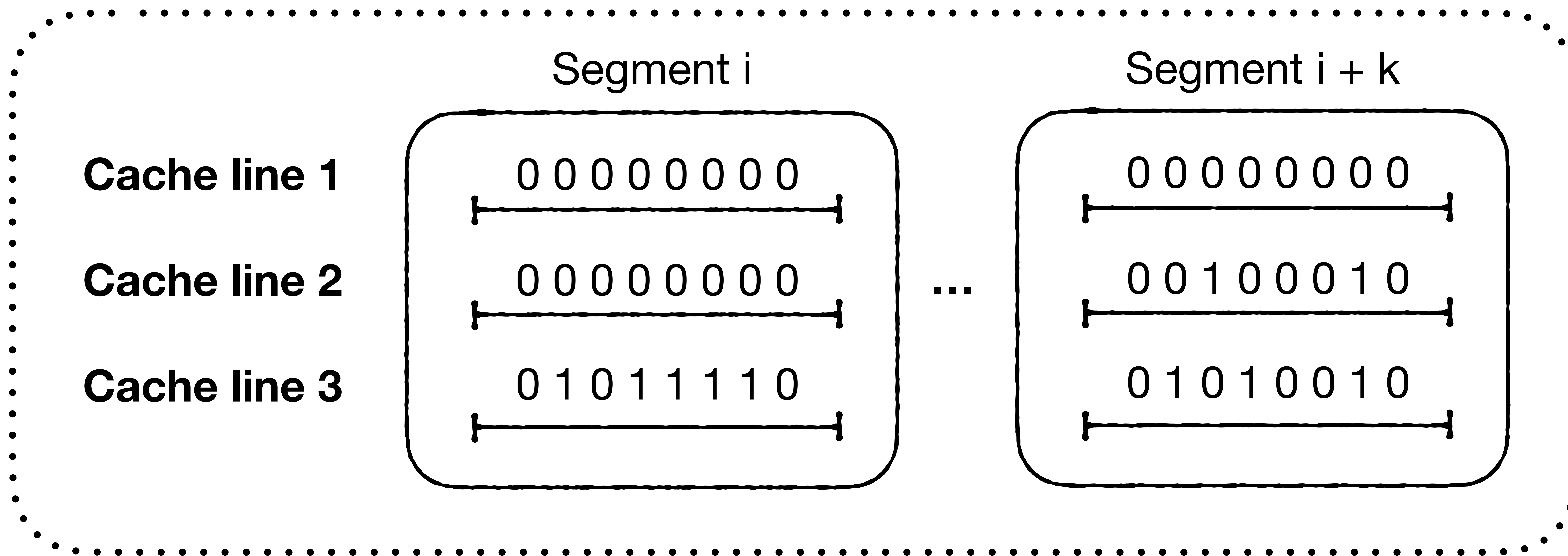


But these still pollute the cache

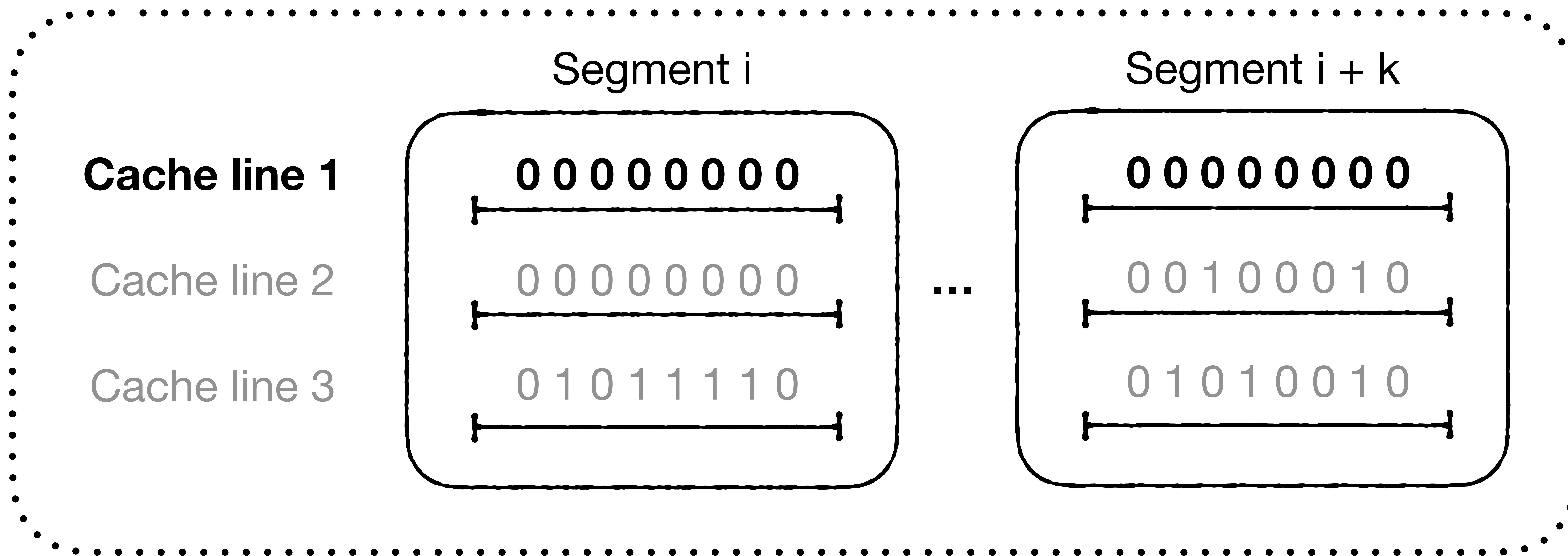
Can we further optimize?

Select * where c > 100

Interleave segments across cache lines :)



Interleave segments across cache lines :)



Ideally, we skip all but the first cache line in this grouping

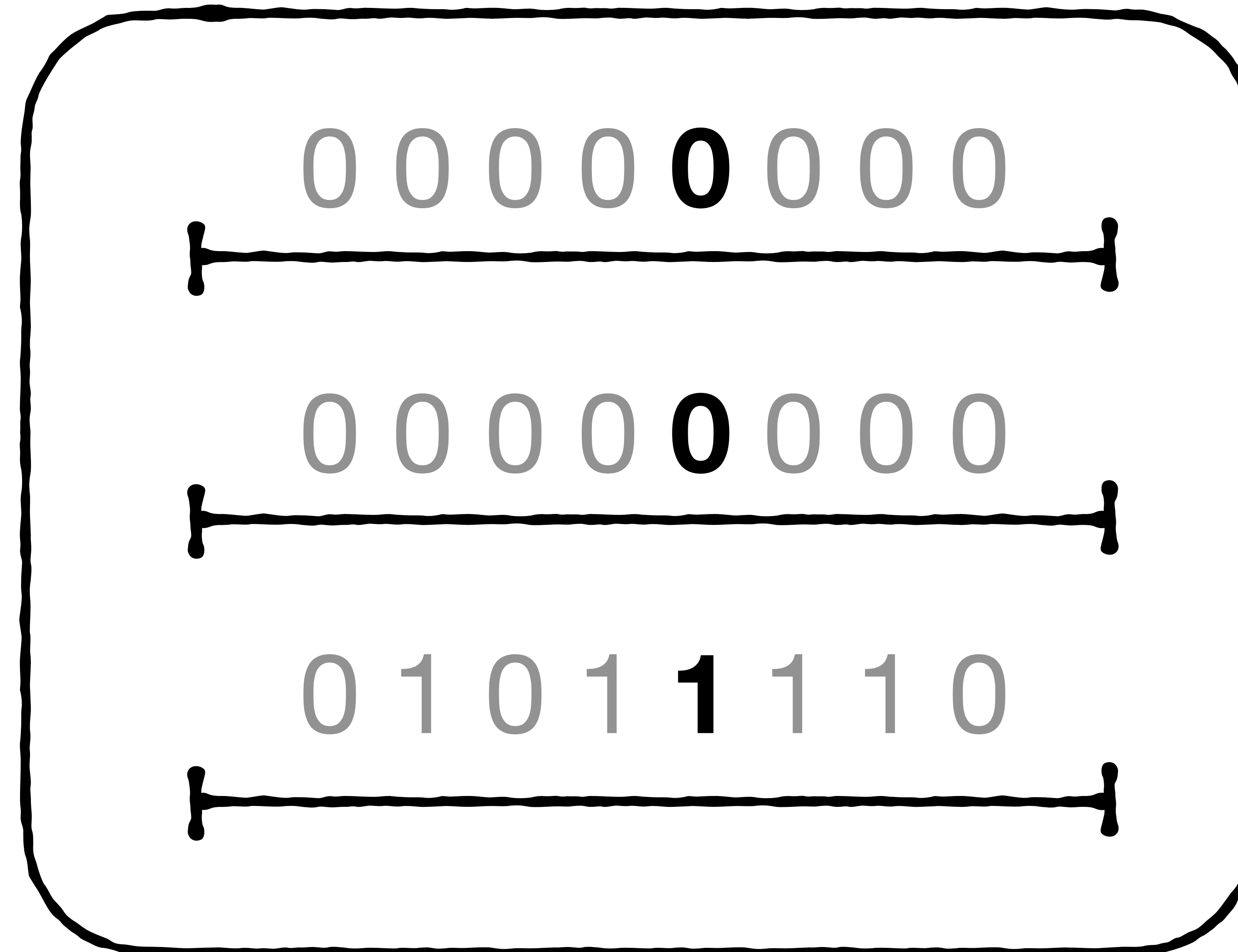
e.g., Select * where c > 100

So far, vertical bitweaving wastes less space than horizontal (no padding or result bits)

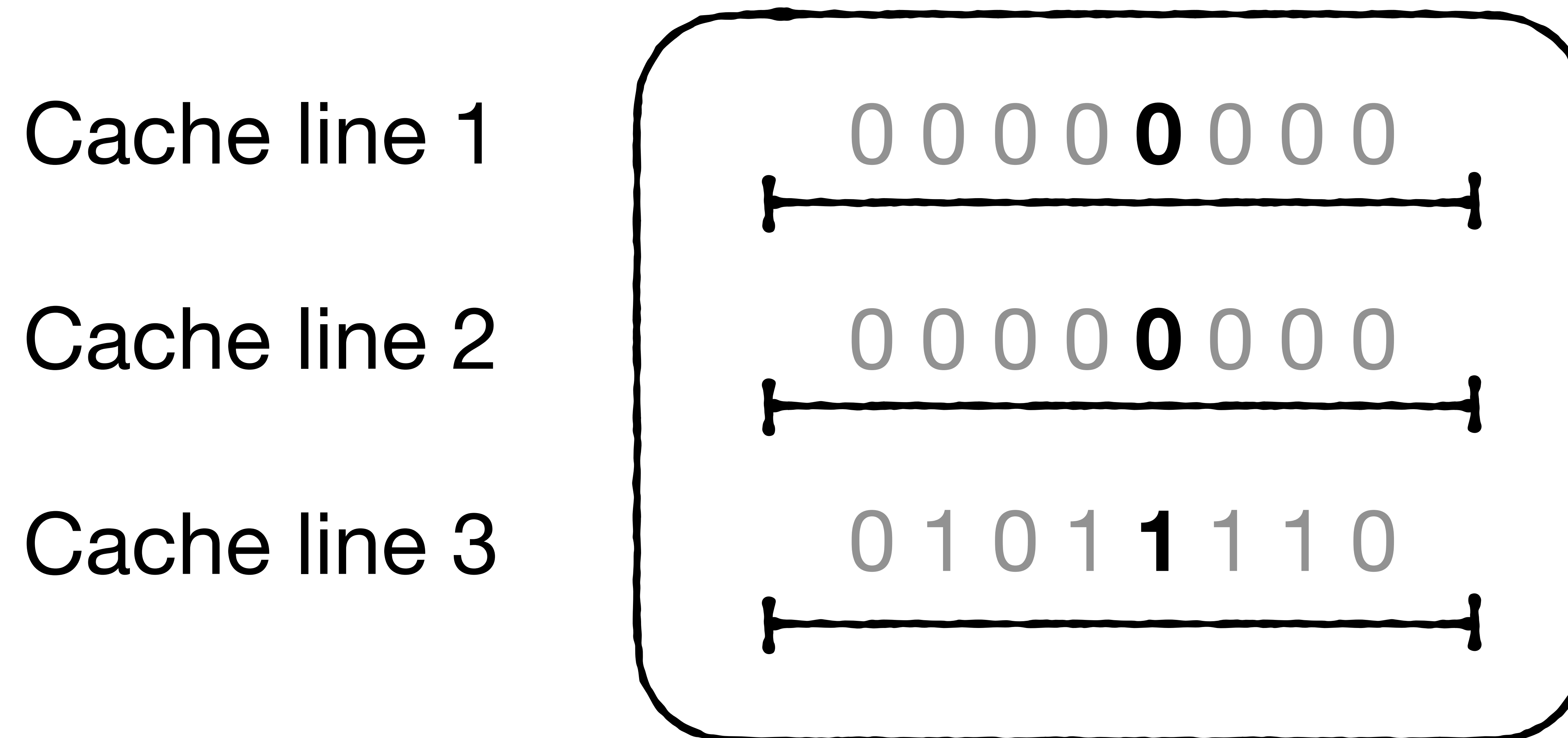
Cache line 1

Cache line 2

Cache line 3

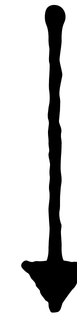


So far, vertical bitweaving wastes less space than horizontal (no padding or result bits)



It also allows early pruning :)

But suppose we wish to get a value at some specific index



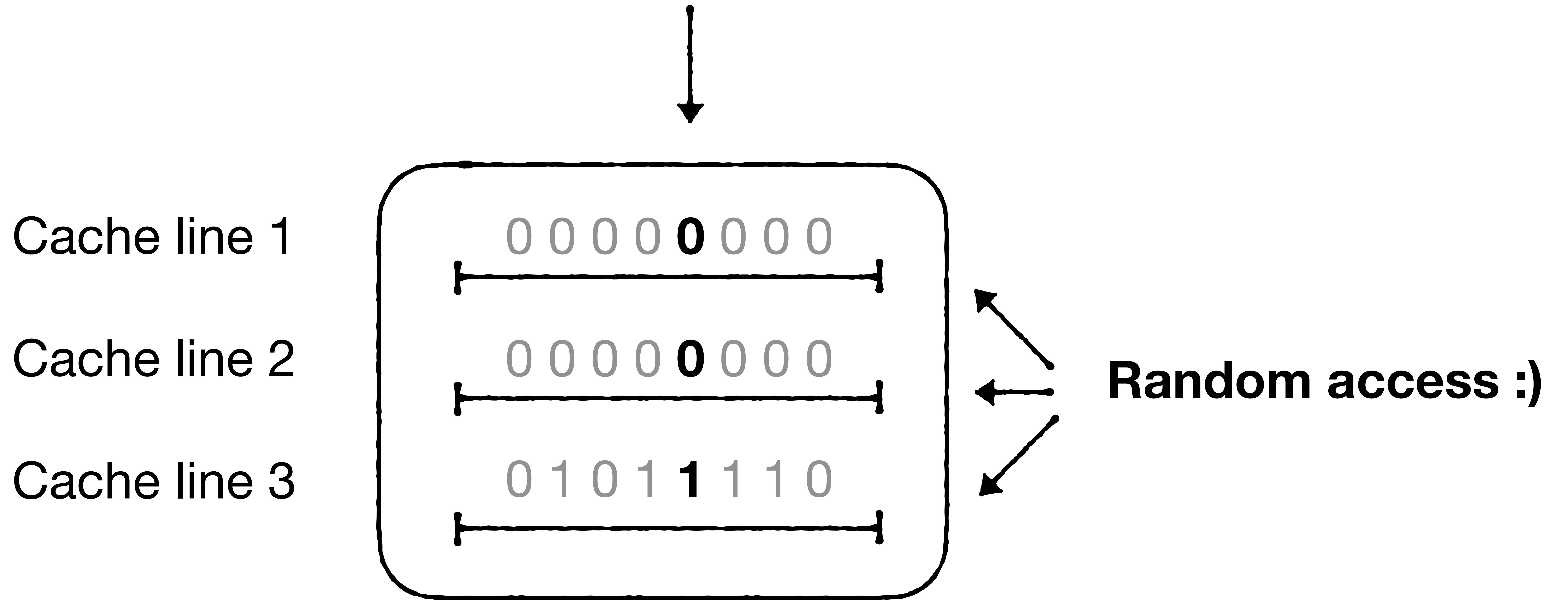
Cache line 1 0 0 0 0 **0** 0 0 0

Cache line 2 0 0 0 0 **0** 0 0 0

Cache line 3 0 1 0 1 **1** 1 1 0

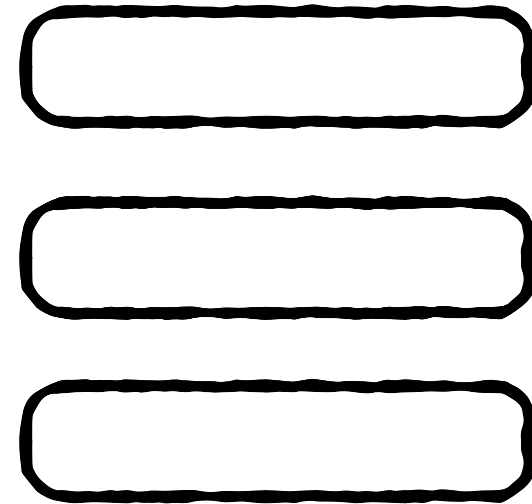
Any issue?

But suppose we wish to get a value at some specific index



BitWeaving Summary

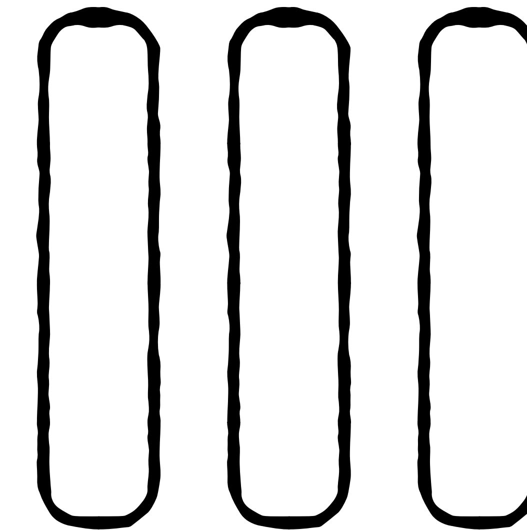
Horizontal



More space

No early pruning

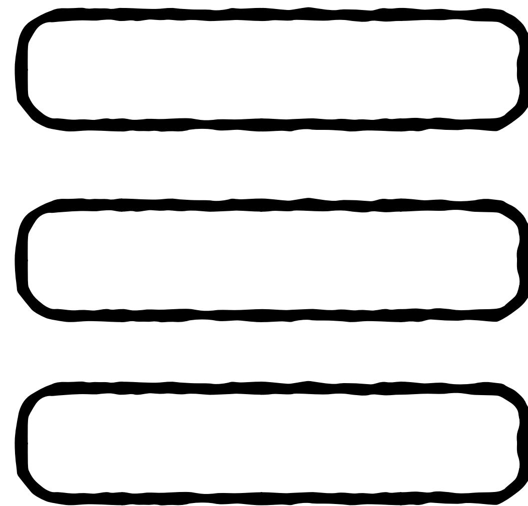
Vertical



Selective value reconstruction entails random I/Os

BitWeaving Summary

Horizontal



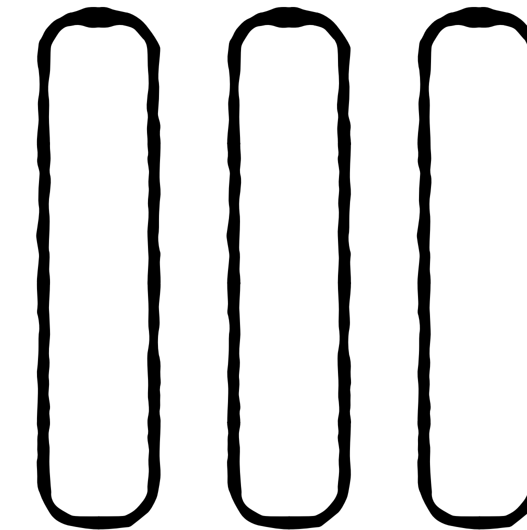
More space

No early pruning

More selective queries

Larger codes

Vertical



Selective value reconstruction entails random I/Os

Less selective queries

Smaller codes

Thank you